

# Jet substructure from ALEPH archived $e^+e^-$ data



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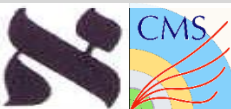
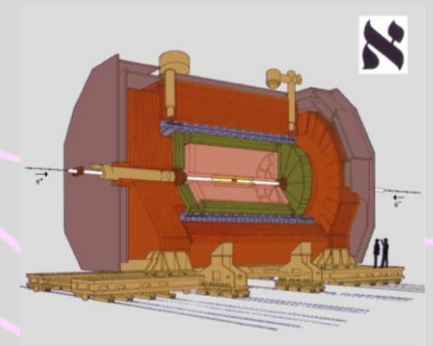
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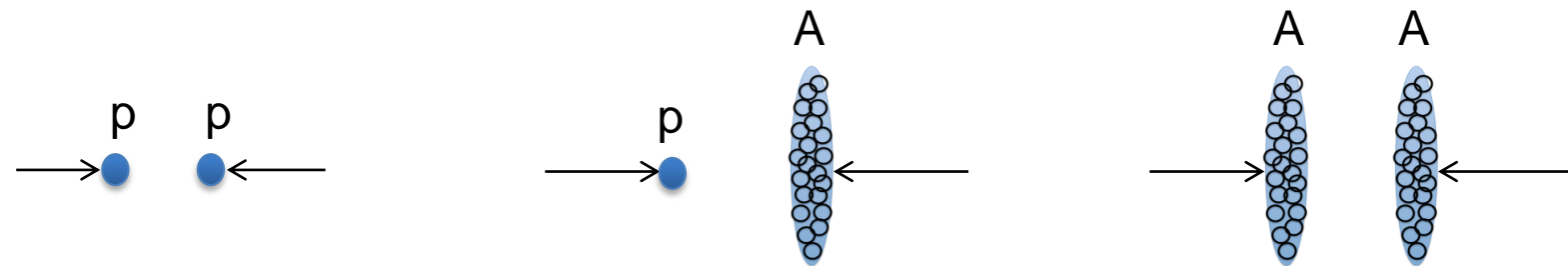
**Jet Physics: From RHIC/LHC to EIC**  
30 June, 2022



# Motivation

- Jets are some of the most powerful tools for the study of Quantum Chromodynamics
- Since the end of LEP operation, significant progress has been made in jet definition and jet algorithms:
  - Jet substructure observables have been widely explored in **pp** and **HI** collisions
  - Novel tools for **jet flavor identification**, **EW boson & top tagging** and **studies of QGP\***
  - However, those techniques are **not yet used in  $e^+ e^-$  annihilation data**
- Monte Carlo generators such as **SHERPA**, **PYTHIA 6**, **PYTHIA 8** and **HERWIG** are tuned with hadronic event shape observables and hadron spectra in  $e^+ e^-$ 
  - Then used to predict the jet spectra and substructure in more complicated hadron collisions

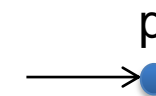
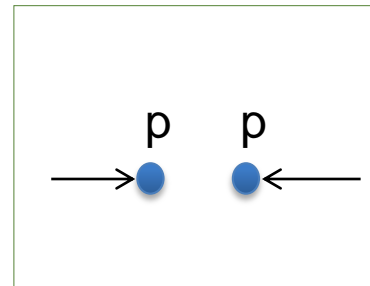
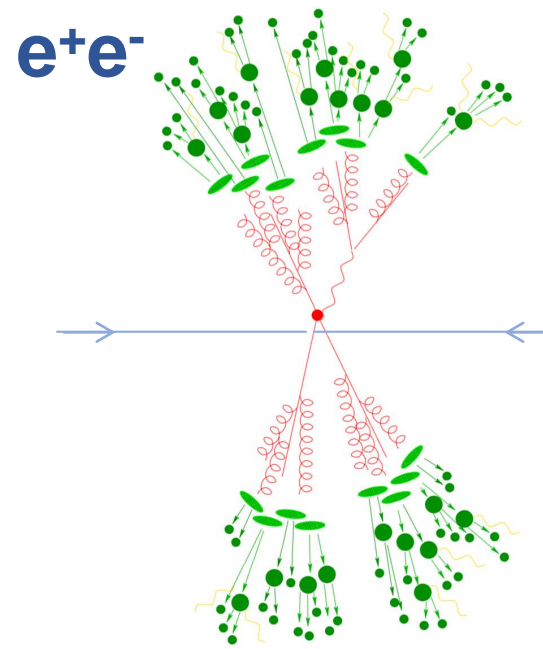
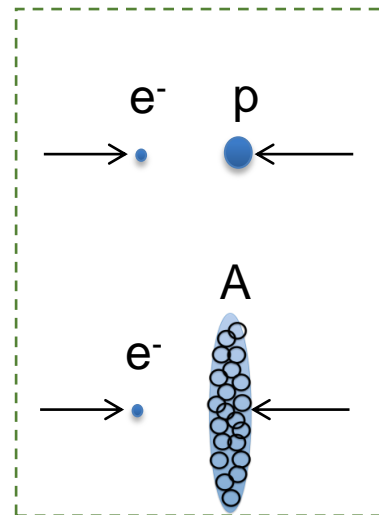
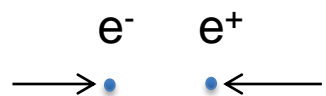
\* H. Andrews et al.  
J. Phys. G, 47(6) 065102, 2020



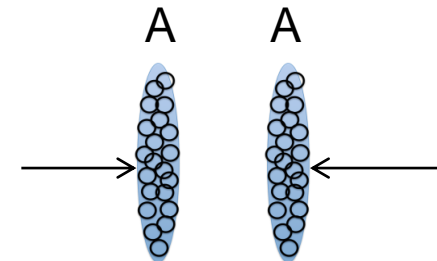
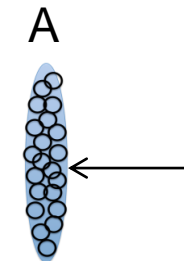
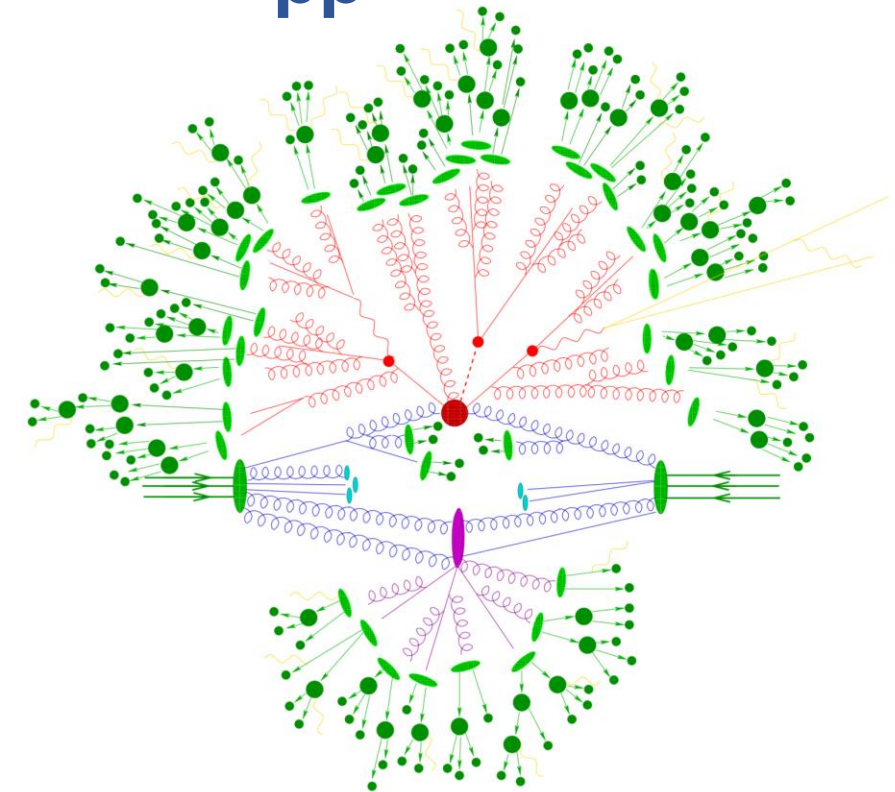
# Jets in Electron-Positron Annihilation

- Jets in  $e^+e^-$  with identical algorithms as those used in hadron colliders are of great interest
  - No gluonic initial state radiation
  - No complications of parton distribution functions
  - No beam remnants and multi-parton interactions

→ **Cleanest test of pQCD and phenomenological models**
- Serve as a reference for the **pp** and future **EIC** measurements
- Inform the QCD studies at the future FCC.

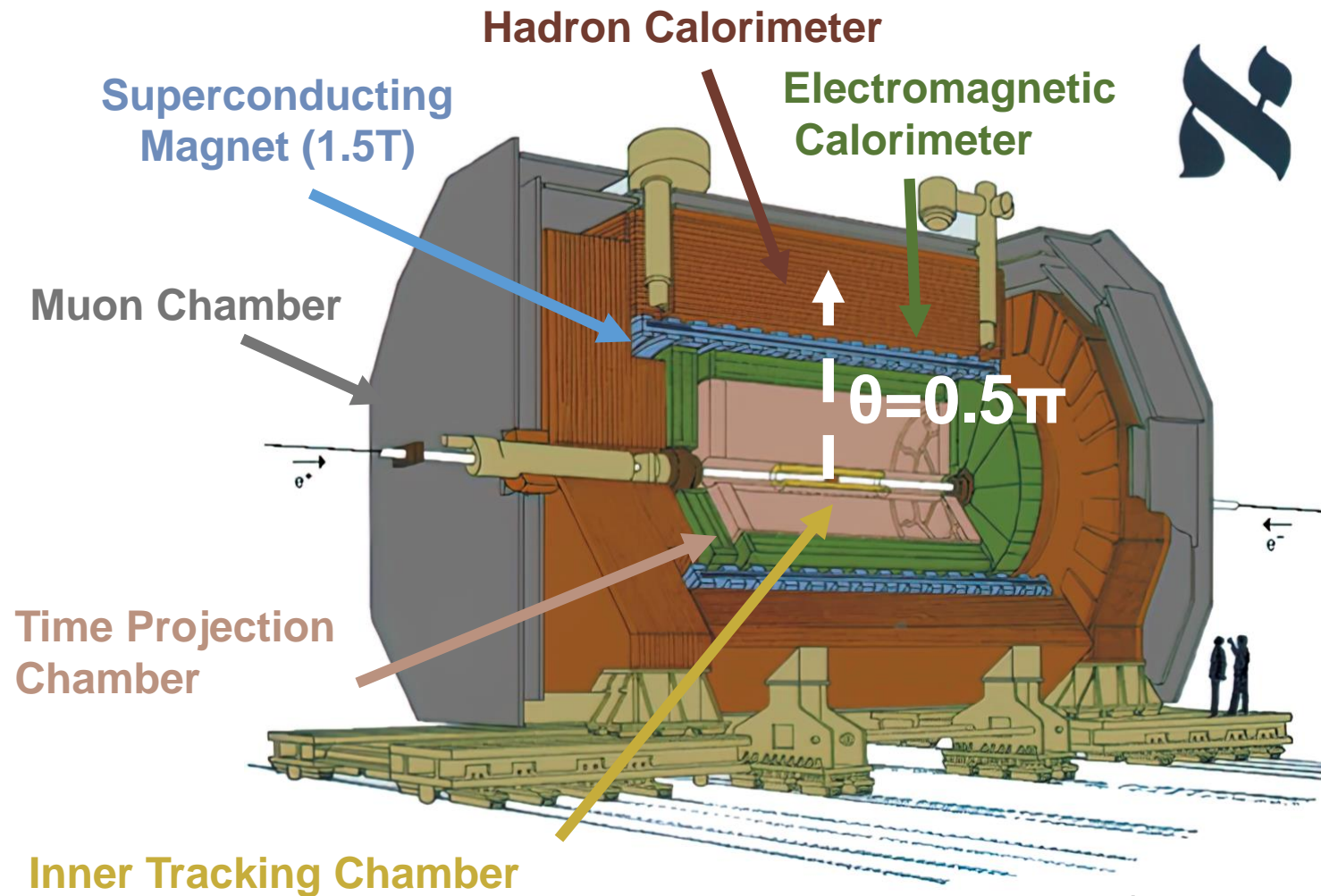


**pp**

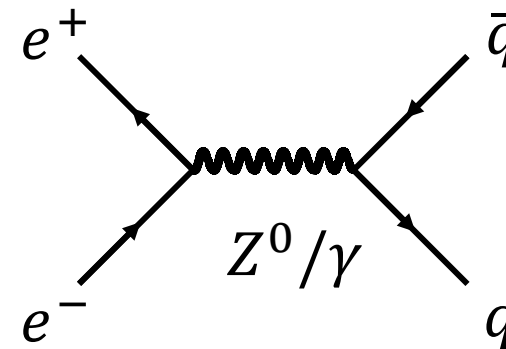




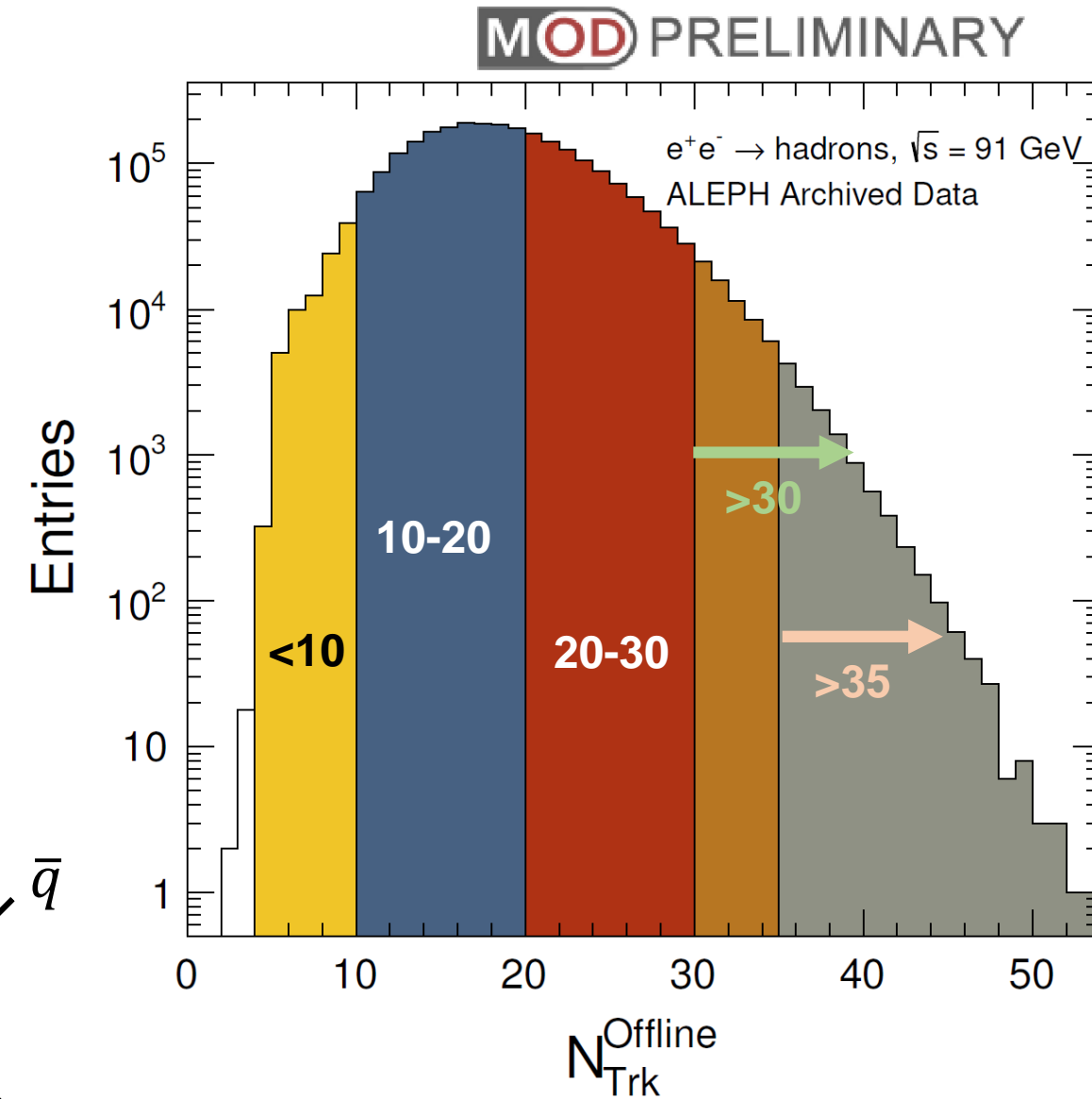
# The ALEPH Detector



- LEP1  $e^+e^-$  data at Z pole (91 GeV) taken between 1992-1995
- Approximately 2.5 million hadronic events are recorded



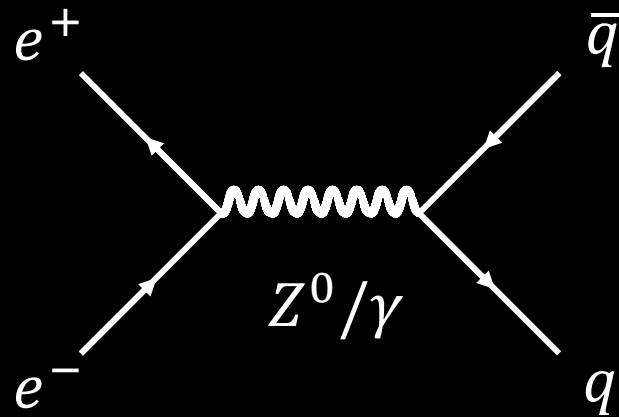
## Charged Particle Multiplicity





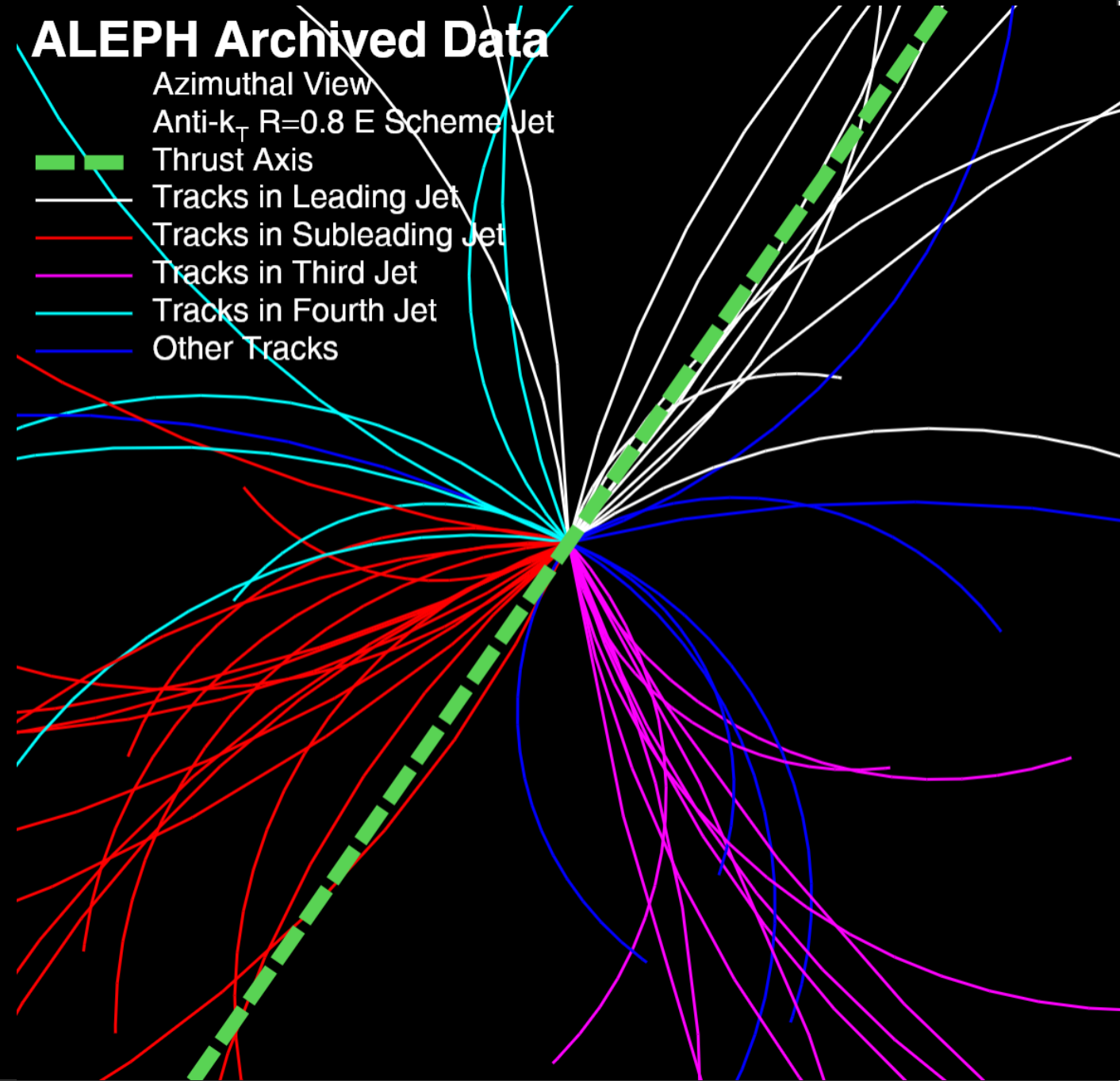
# High Multiplicity Event in $e^+e^-$ Collisions

Highest multiplicity event in ALEPH LEP1 data  
Collision Energy = 91 GeV



## ALEPH Archived Data

- Azimuthal View
- Anti- $k_T$   $R=0.8$  E Scheme Jet
- Thrust Axis
- Tracks in Leading Jet
- Tracks in Subleading Jet
- Tracks in Third Jet
- Tracks in Fourth Jet
- Other Tracks



+ YJL

arXiv: 1906.00489  
PRL 123, 212002 (2019)

55 Charged Particles  
Thrust  $T=0.71$

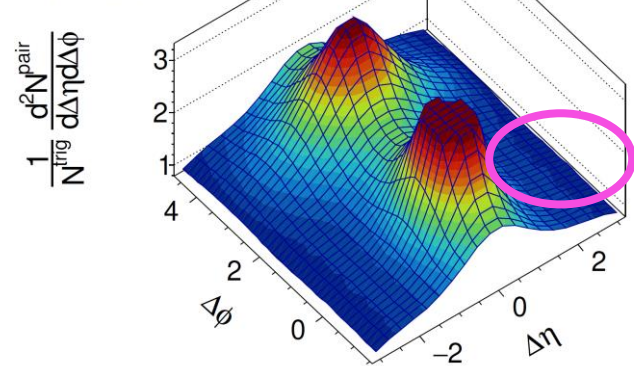
# Two-Particle Correlation Function from ALEPH $e^+e^-$ at 91 GeV

ALEPH  $e^+e^- \rightarrow \text{hadrons}$ ,  $\sqrt{s} = 91 \text{ GeV}$

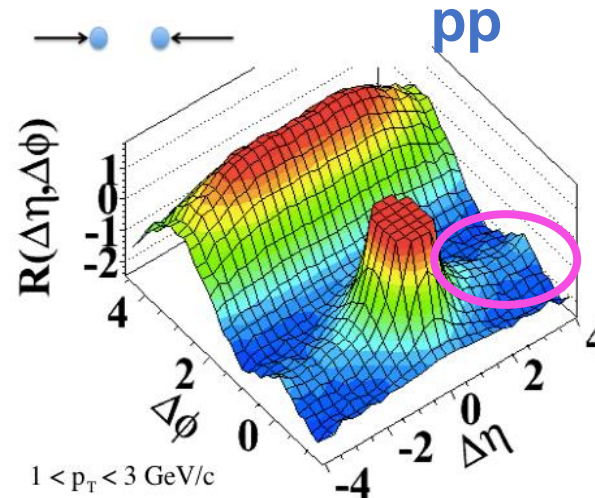
$N_{\text{Trk}}^{\text{Offline}} \geq 35$ ,  $|\cos\theta| < 0.9$

$p_T^{\text{lab}} > 0.2 \text{ GeV}$

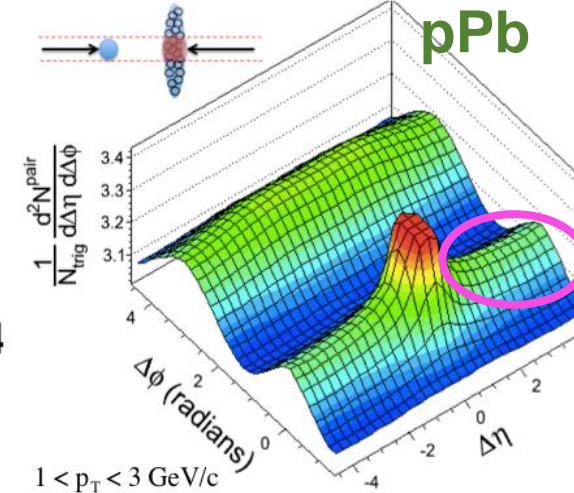
Thrust coordinates



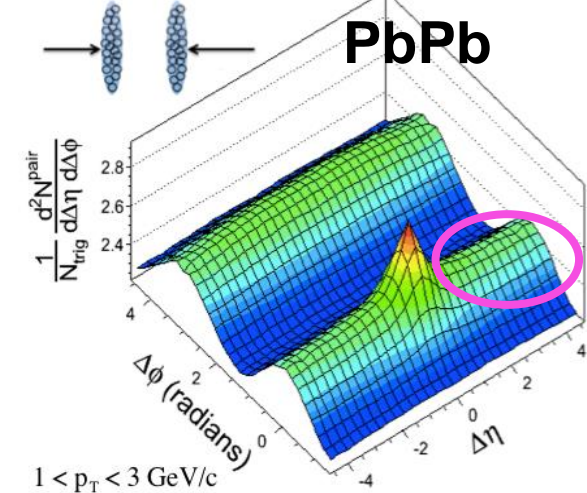
pp  $\sqrt{s} = 7 \text{ TeV}$ ,  $N_{\text{Trk}}^{\text{Offline}} \geq 110$



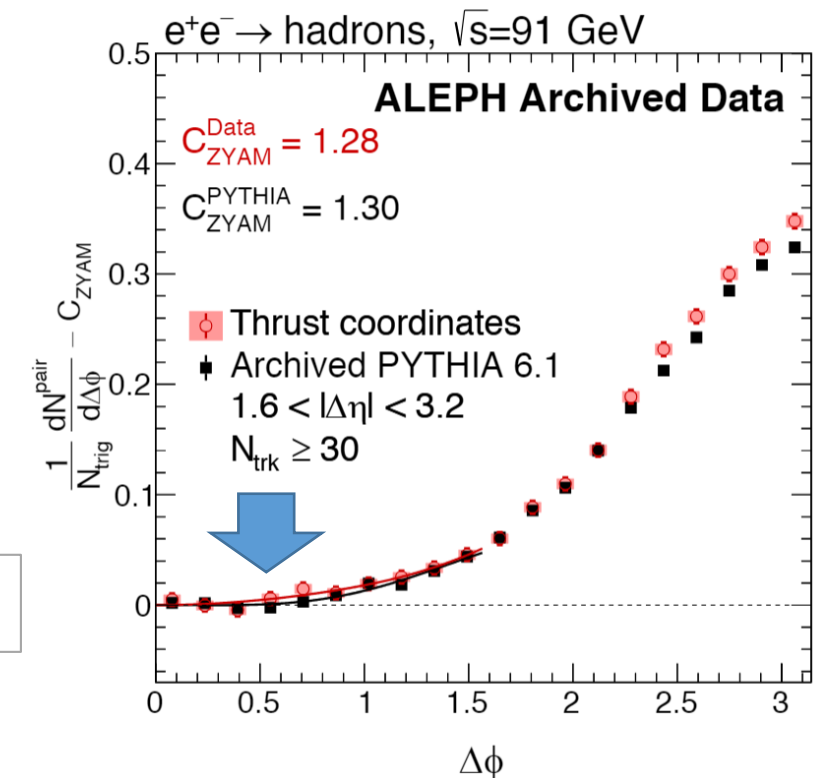
pPb  $\sqrt{s_{NN}} = 5.02 \text{ TeV}$ ,  $220 < N_{\text{Trk}}^{\text{Offline}} \leq 260$



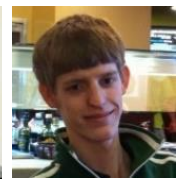
PbPb  $\sqrt{s_{NN}} = 2.76 \text{ TeV}$ ,  $220 < N_{\text{Trk}}^{\text{Offline}} \leq 260$



- **No sign of ridge signal** in electron-positron collisions up to  $\sim 55$  charged particles per event
- **New reference to the collective behavior** in small collision systems!



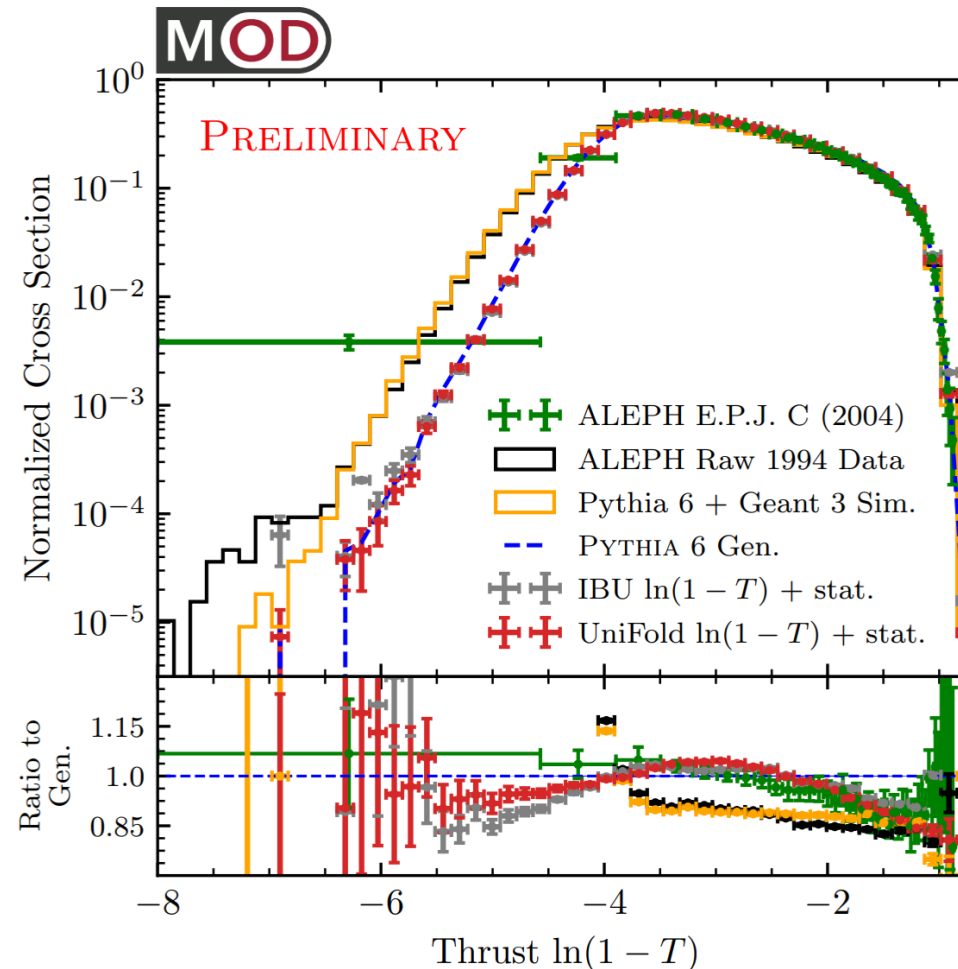
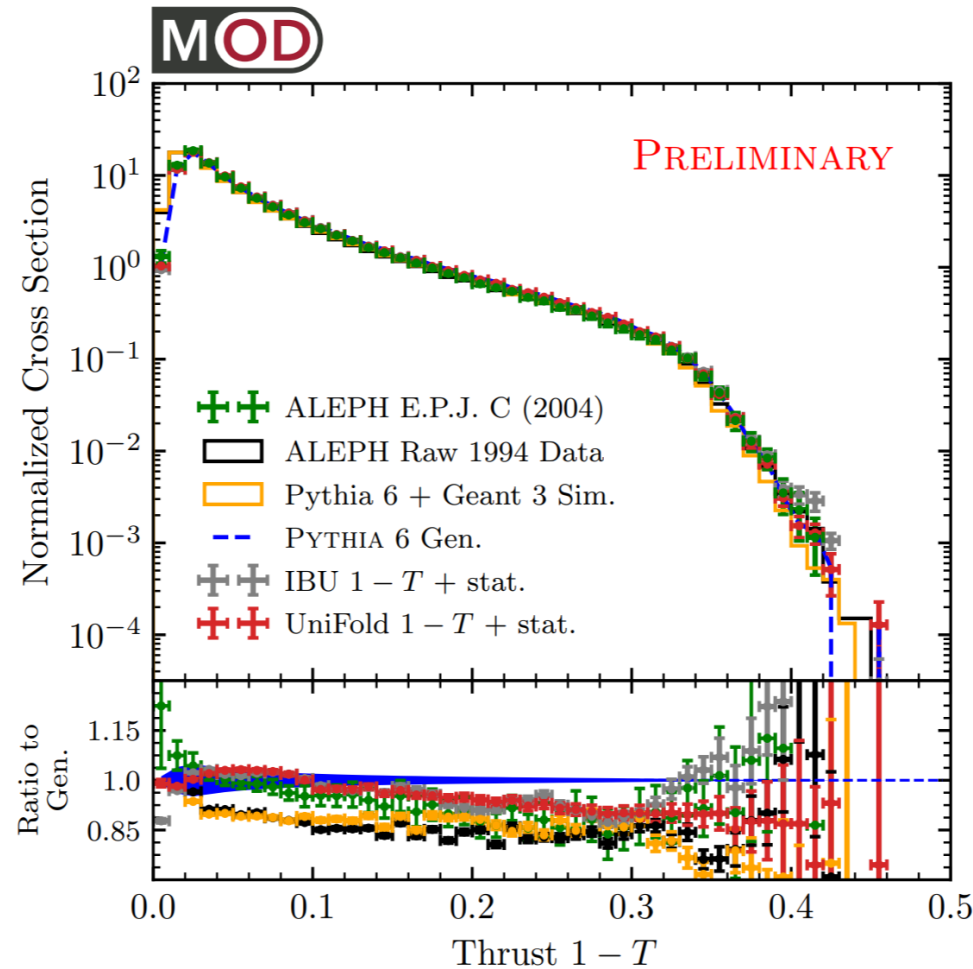
arXiv: 1906.00489  
PRL 123, 212002 (2019)



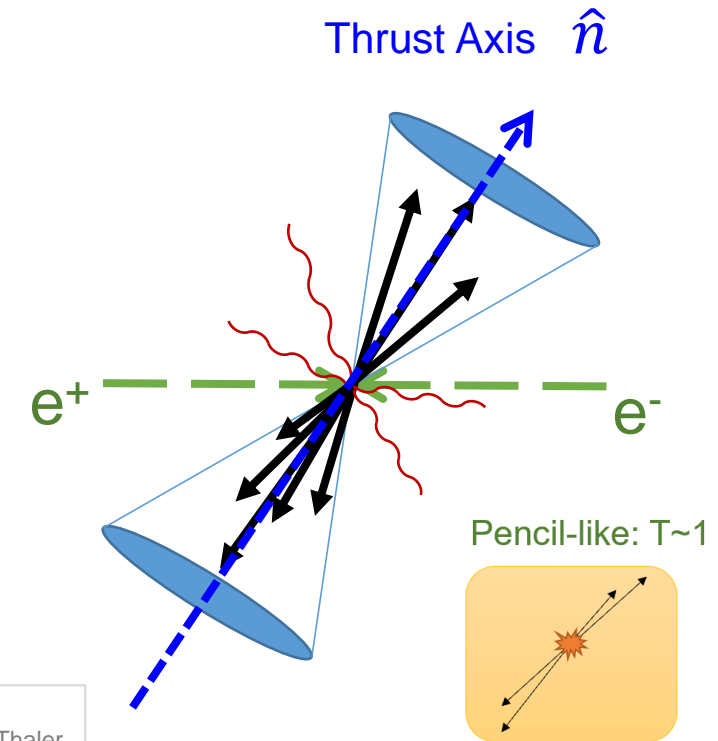
+ YJL



# Unfolded Thrust Distribution



$$T = \max_{\hat{n}} \frac{\sum_i |\hat{p}_i \cdot \hat{n}|}{\sum_i |\hat{p}_i|}$$



- Unfolded results consistent with ALEPH publication in 2004

EPJC 35 (2004) 456

- New differential measurement in the small **1-T** region (pencil-like event)

Paper in preparation

OmniFold algorithm: PRL 124, 182001  
Andreassen, Komiske, Metodiev, Nachman, Thaler



Anthony Badea



Patrick T. Komiske III



Eric Metodiev



Jesse Thaler



Ben Nachman

+ YJL

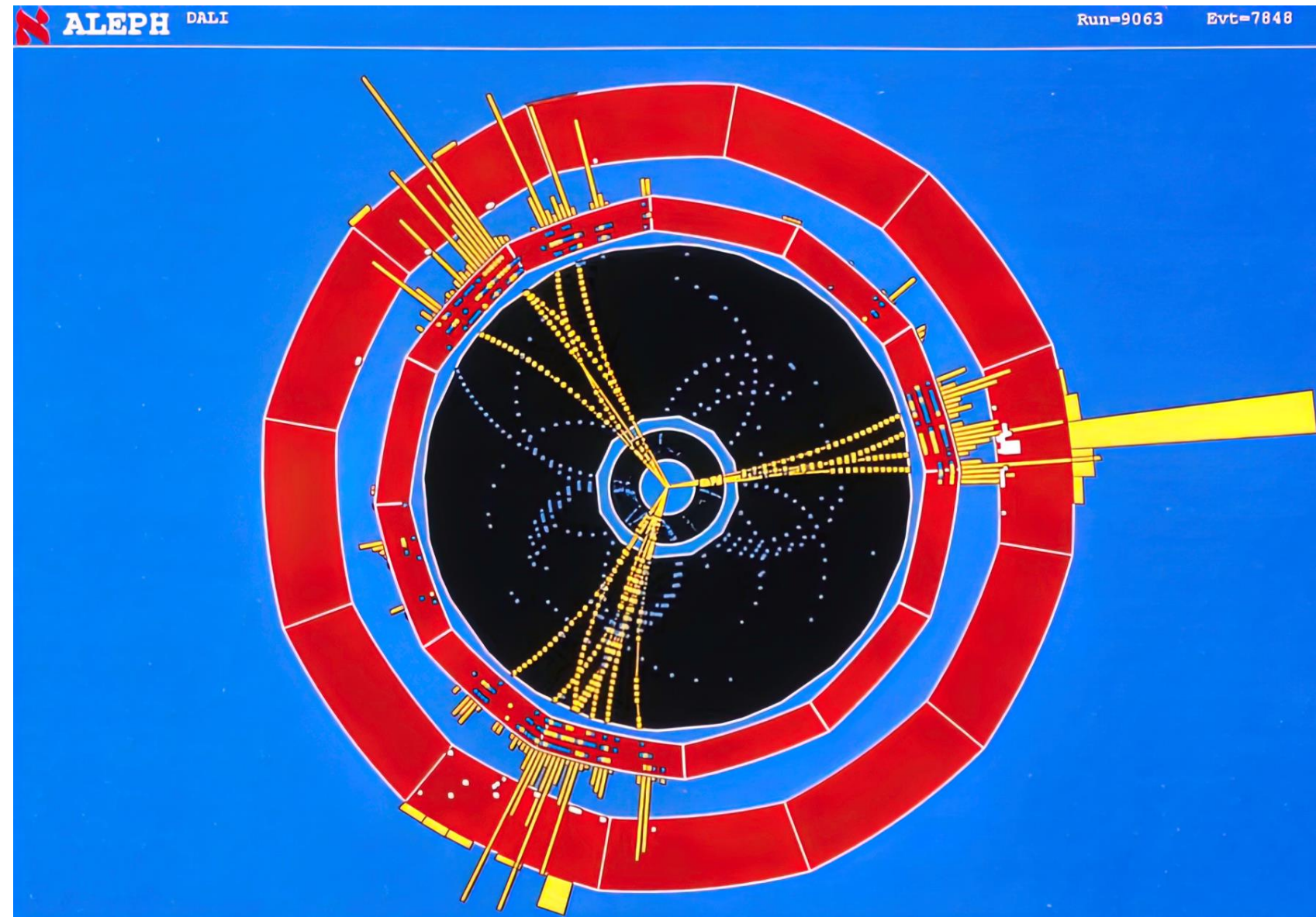


# Jet Reconstruction

- ALEPH archived data and MC from **1994** is used for this analysis
- Identical hadronic  $Z^0$  decay selection as the correlation function paper and ALEPH QCD papers
- Jets are reconstructed with an “**anti- $k_T$** ” **algorithm** with  $R_0=0.4$  using energy-flow objects identified with trackers, calorimeters and muon chambers.
- Note that the distance metric is defined by jet energy (E) and jet angle ( $\theta$ ):

$$d_{ij} = \min(E_i^{-2}, E_j^{-2}) \frac{1 - \cos \theta_{ij}}{1 - \cos R_0}$$
$$d_{iB} = E_i^{-2},$$

where  $\theta_{ij}$  is the **actual opening angle** between  $i^{\text{th}}$  and  $j^{\text{th}}$  pseudojets

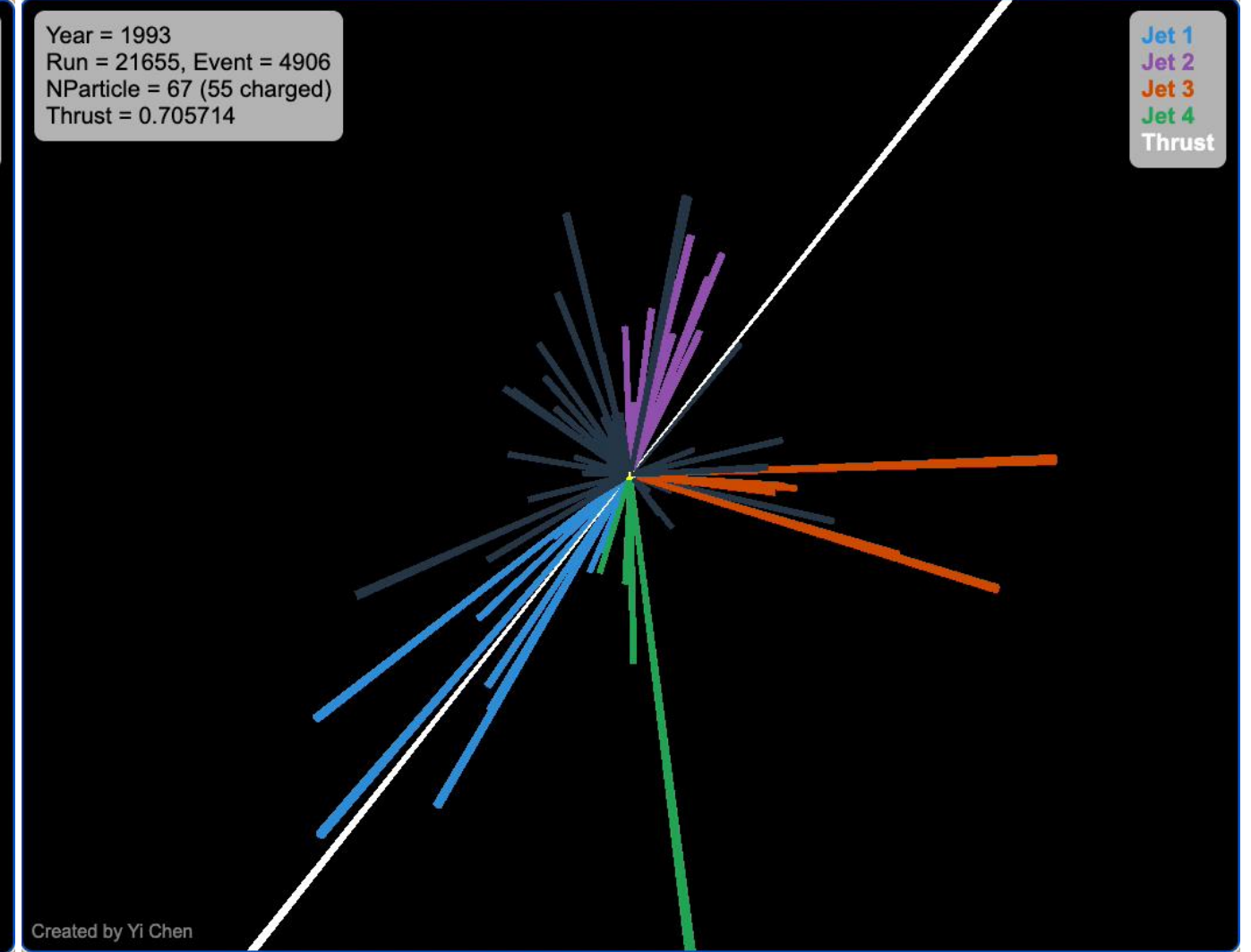
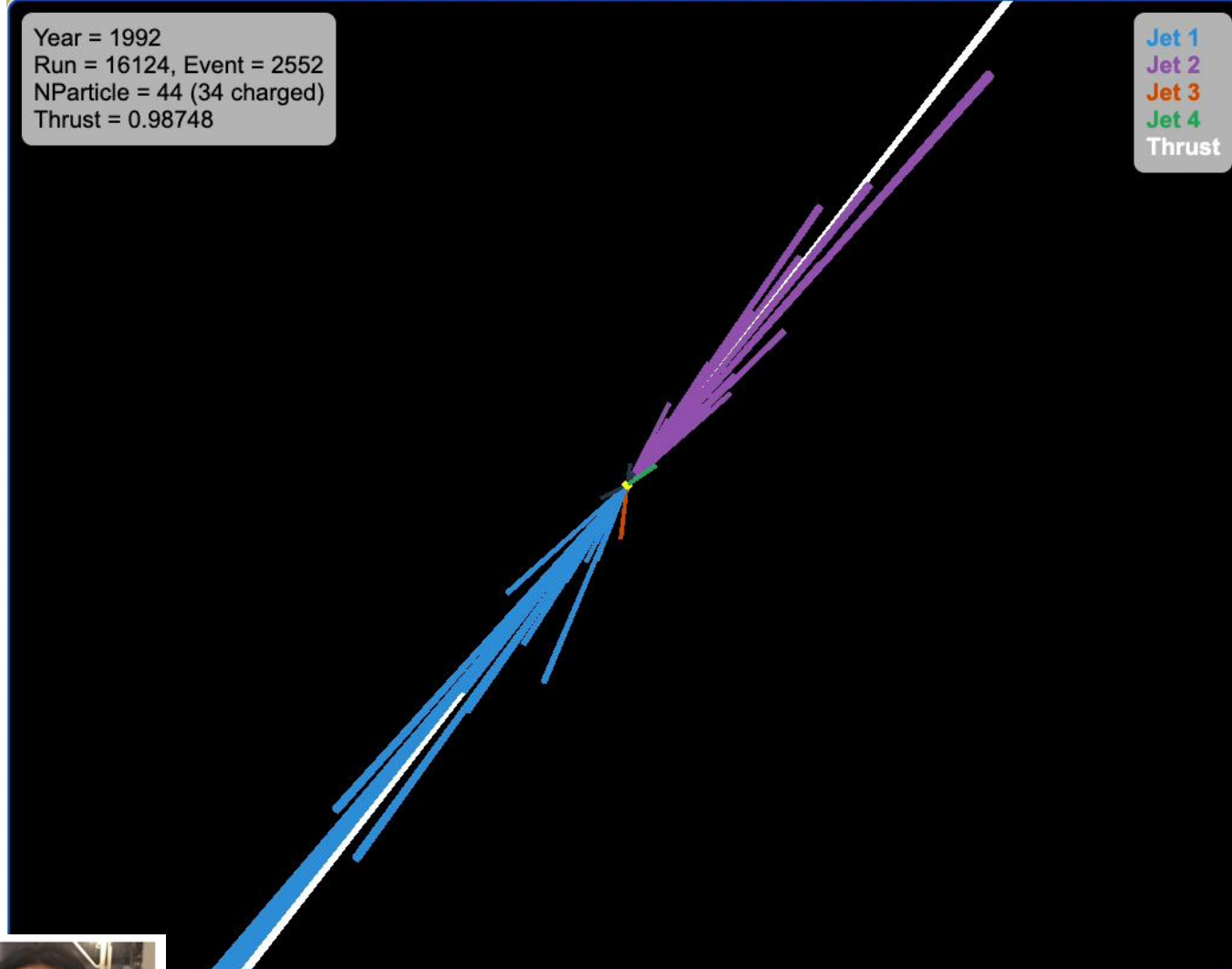


ALEPH Event Display

Anti- $k_T$  : [JHEP 04 \(2008\) 063](#)

TPC paper: PRL 123, 212002 (2019)  
QCD paper: EPJC 35 (2004) 456

# Jet Events at LEP

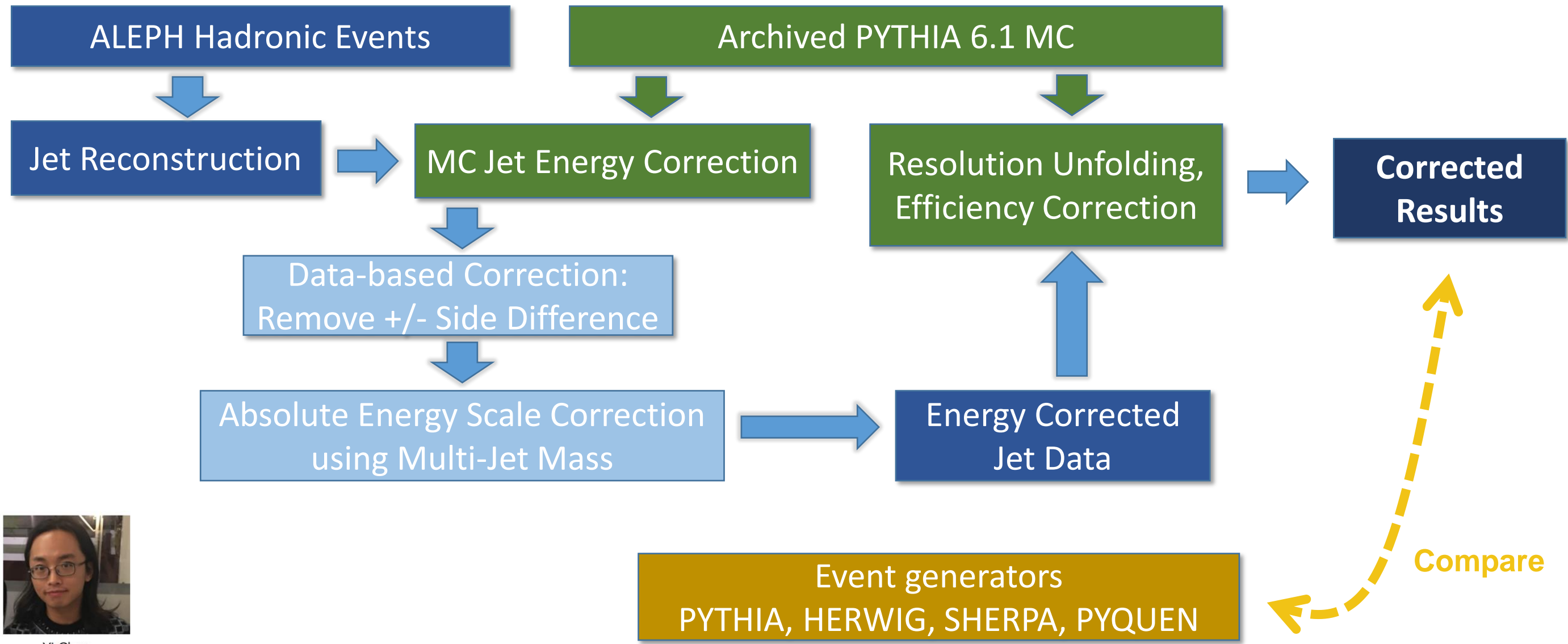


Created by Yi Chen



Yi Chen  
(MIT, CMS)

# Jet Analysis with Archived ALEPH data



Yi Chen  
(MIT, CMS)



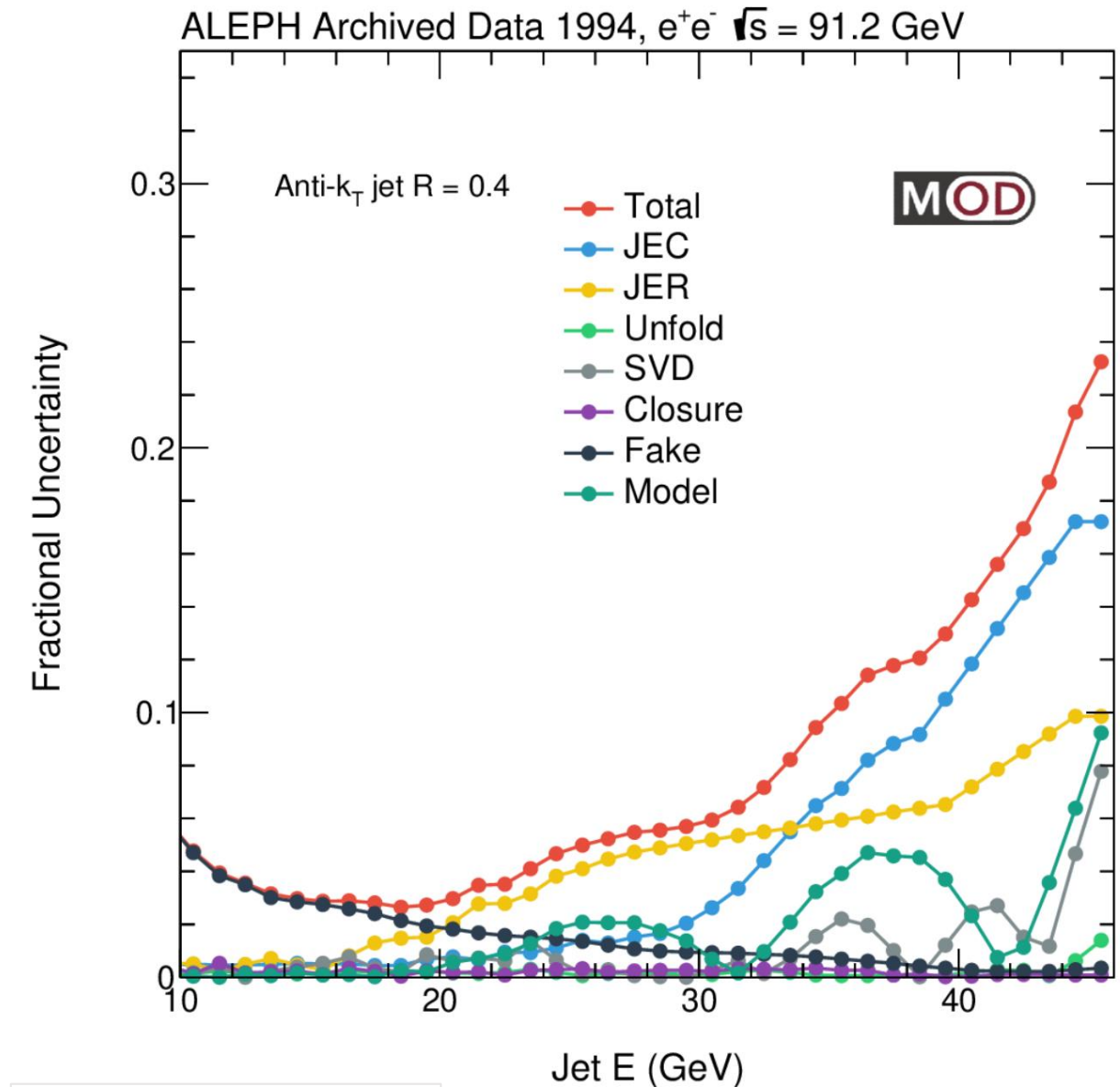
# Systematic Uncertainties

For inclusive jet analyses:

- **Jet energy scale**: vary the energy scale by  $\pm 0.5\%$
- **Jet resolution**: vary the resolution scale factor by  $\pm 2.5\%$
- **“Fake jets”**: accidental clusters of energy in the final state that do not correspond to an initial high energy parton
- **Unfolding**: choice of prior, regularization and **unfolding method**
- **Variation of Models**: data-driven reweighting & subjet angle and energy smearing
- **Any non-closure** in MC studies

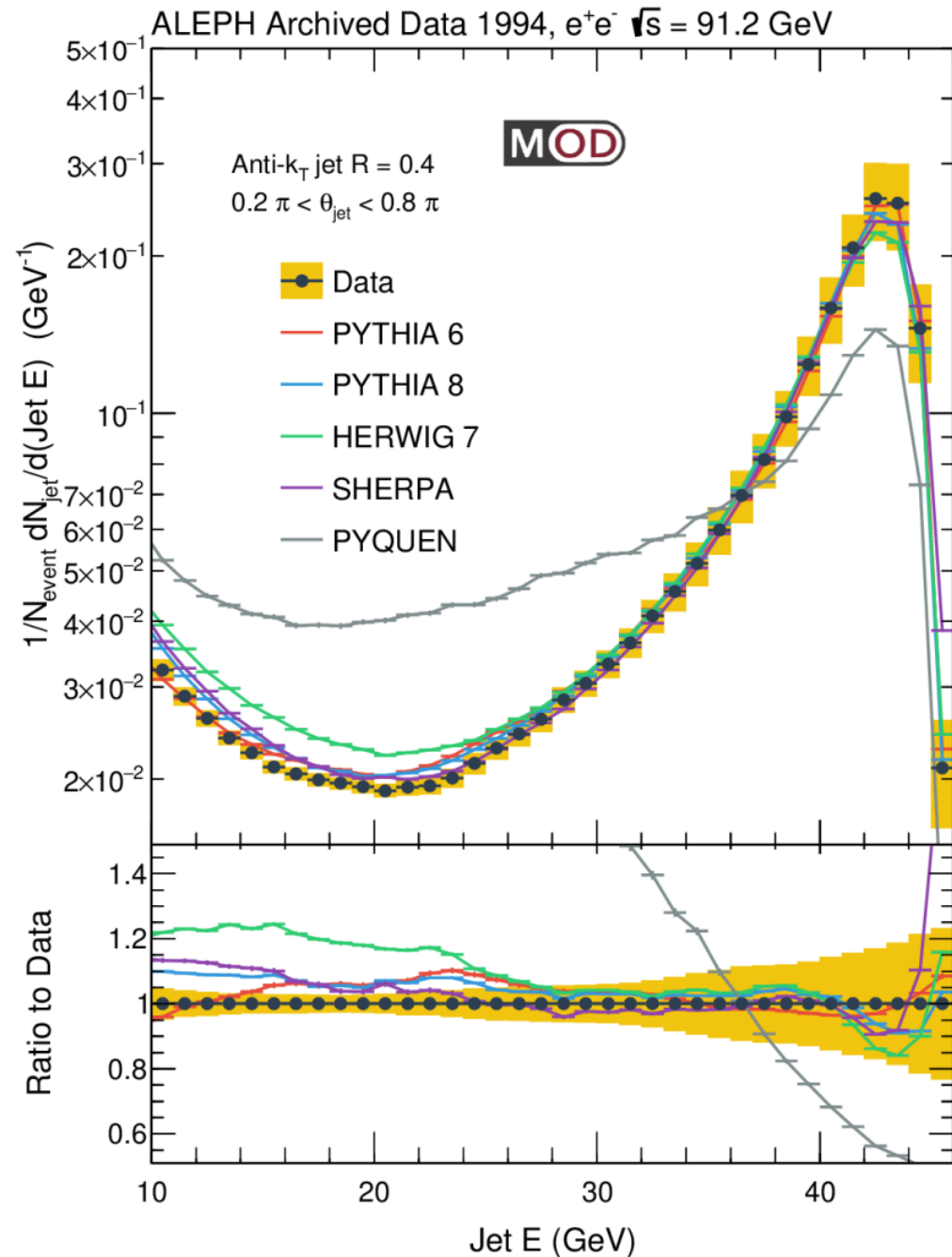
For leading dijet analysis: following additional items:

- **The total energy selection** (to ensure both jets are in the acceptance) is varied to change the purity between 98%- 99.5%.
- **Efficiency correction factor** on jet spectrum are derived using a reweighted MC and the difference is quoted as systematics

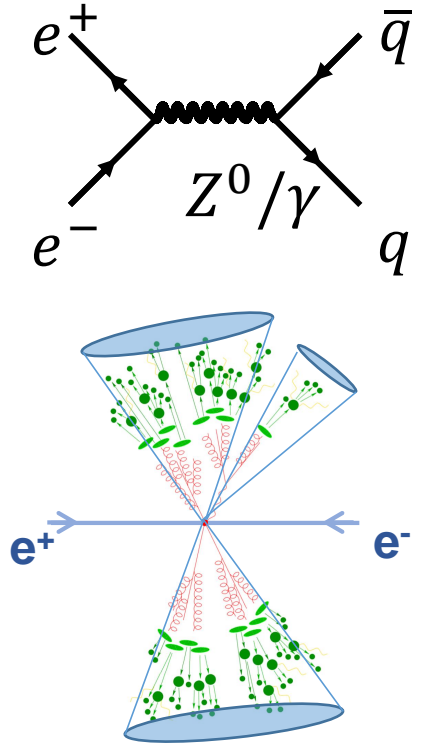


MITHIG-MOD-21-001  
[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
JHEP 06 (2022) 008

# Inclusive Jet Spectrum vs. Generators

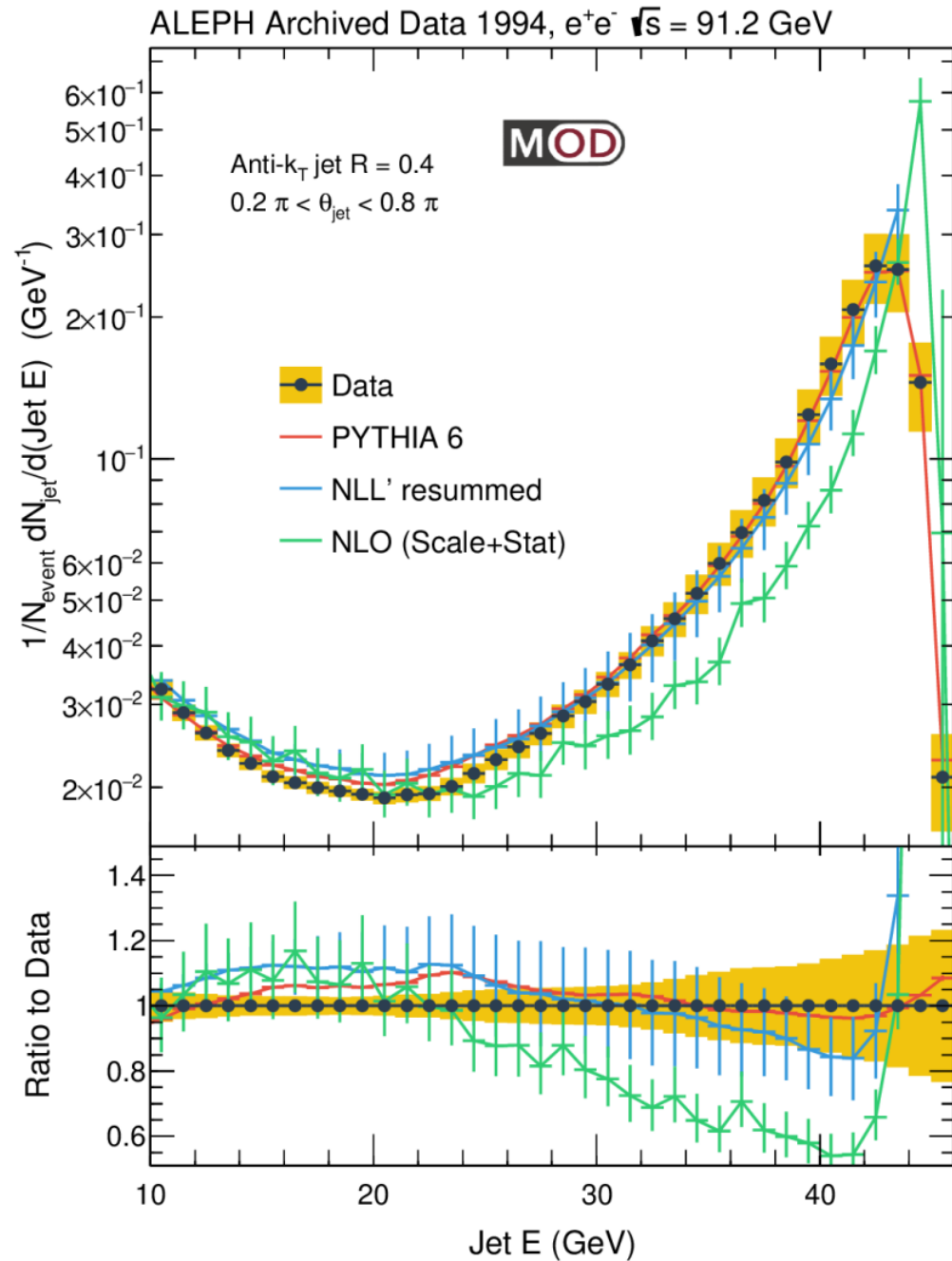


- The closest observable to the jet spectra analyses in hadron-hadron collisions!
- Peak at around 43 GeV: from  $Z \rightarrow q\bar{q}$  and parton shower of the (anti-)quark **almost fully captured** by the jet clustering
- Minimum at around 20 GeV
- At low E: increase due to a large number of jets from **soft emissions** or **combinatorial**
- SHERPA**, **PYTHIA 6**, **PYTHIA 8** and **HERWIG** capture those general features, overpredict the **data** at low jet E
- PYQUEN** (with **energy loss** in minimum-bias PbPb at 5.02 TeV) produce a lot more low energy jets



MITHIG-MOD-21-001  
[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
 JHEP 06 (2022) 008

# Inclusive Jet Spectrum vs. NLO Calculation

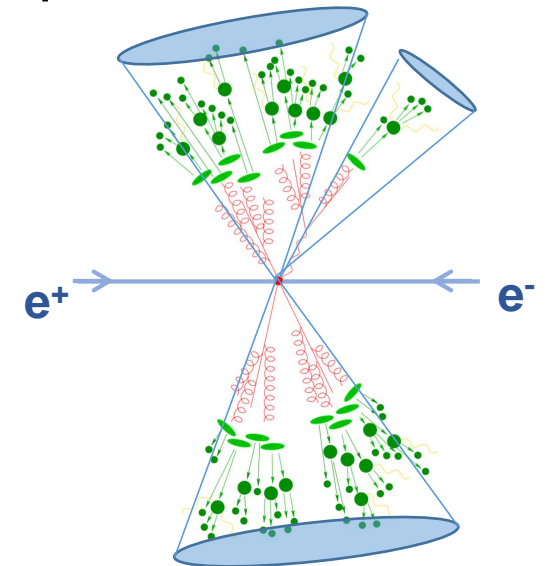
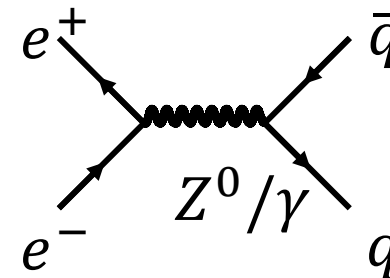


- LO calculation in parton level gives trivial result:

a delta function at  $E = \frac{M_Z}{2}$

- The experimental **data** is wider than predictions from an **NLO calculation in parton level\***
- Next-to-leading logarithmic (NLL') threshold and jet radius resummation\*\* give a reasonable description of data

The same data as previous slide



\*NLO calculation from João Pires (LIP)

\*\*NLL'+R calculation from Duff Neill, Felix Ringer, Nobuo Sato

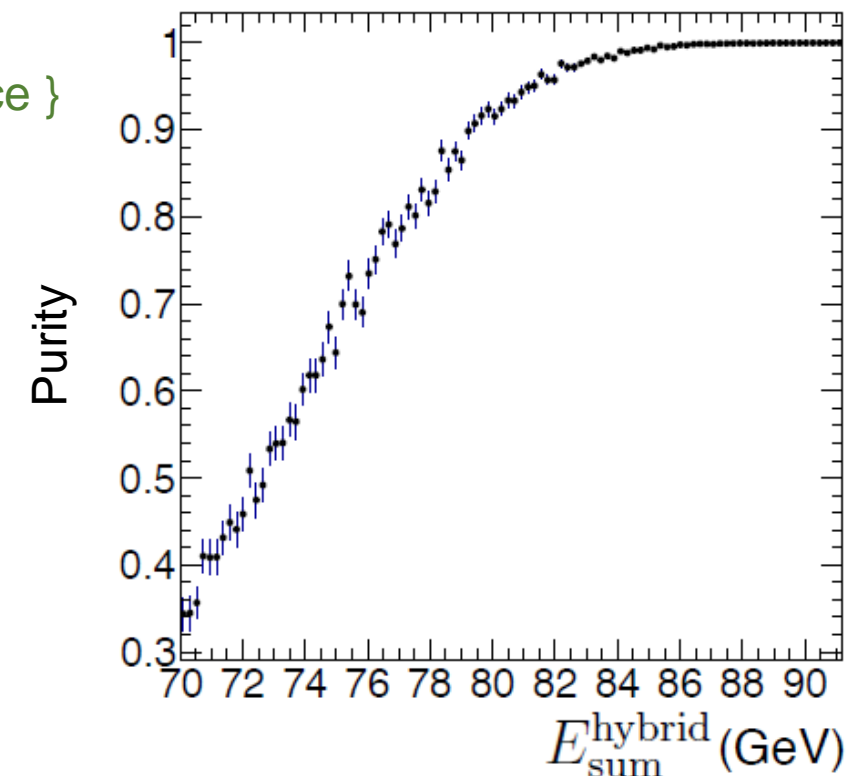
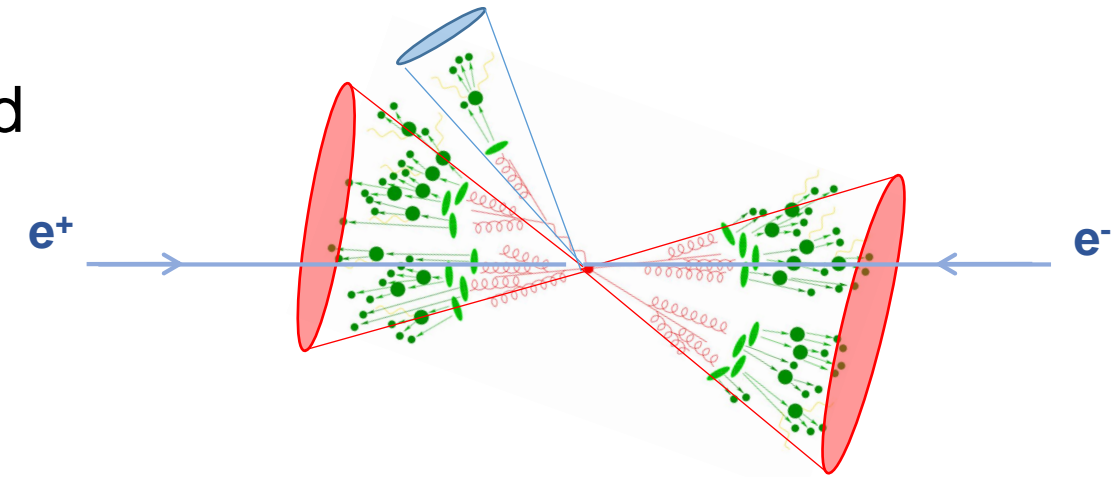


# Leading Dijet Selection

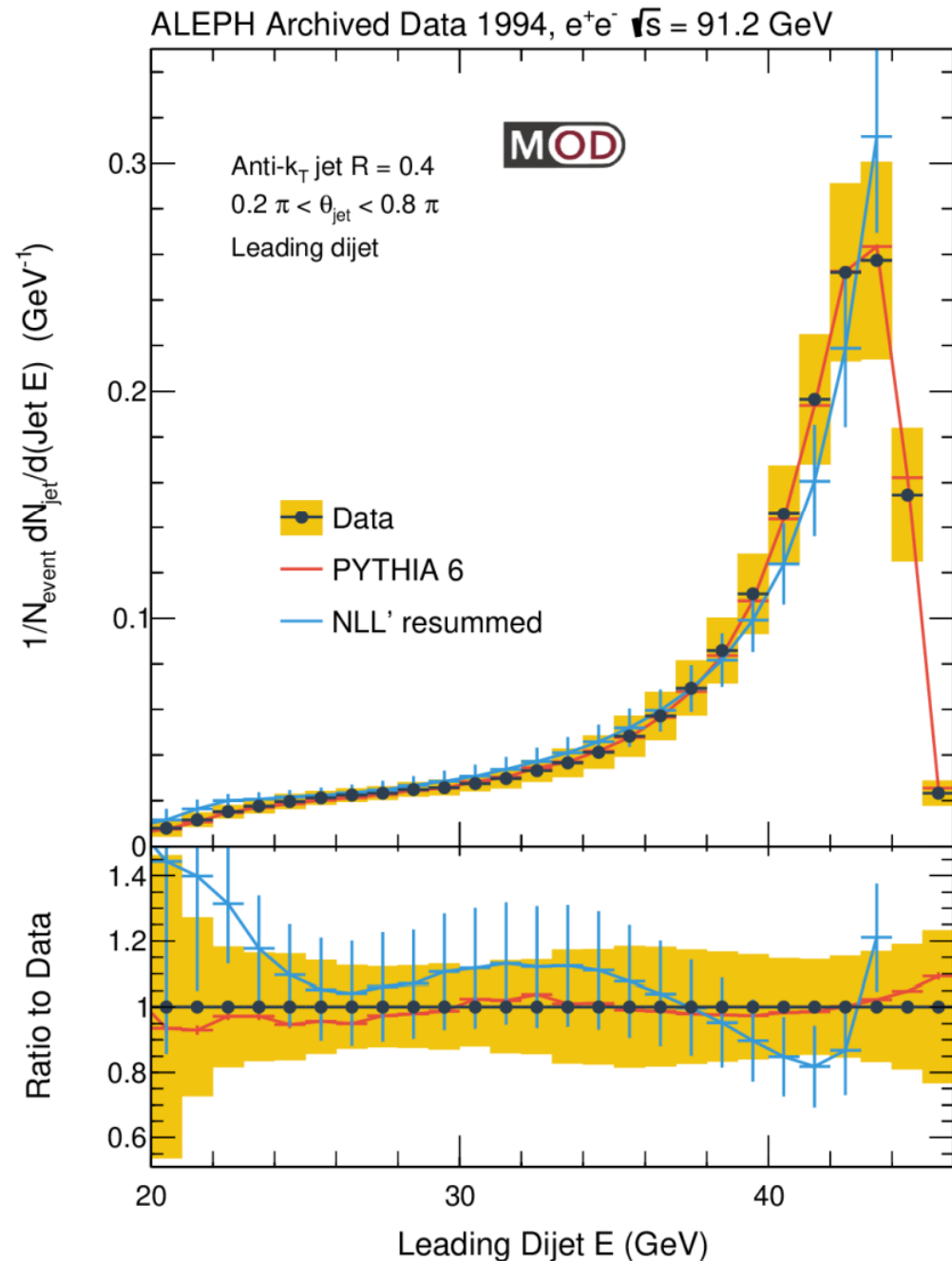
- When the **global leading jets** overlap with the dead region (close to beam), some of the jet energy will not be detected and they may **appear as low energy jets**.
- A hybrid total energy observable is constructed to select events which have both leading jets in the acceptance:

$$E_{\text{sum}}^{\text{hybrid}} = \text{Energy sum of } \{ \text{Particles within acceptance } 0.2\pi < \theta < 0.8\pi \} \\ \cup \{ \text{Particles with angle } < 0.4 \text{ to axes of any jet above 5 GeV in the acceptance} \}$$

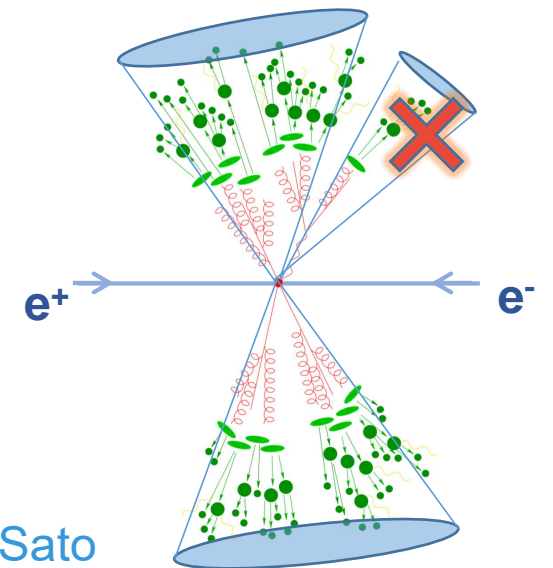
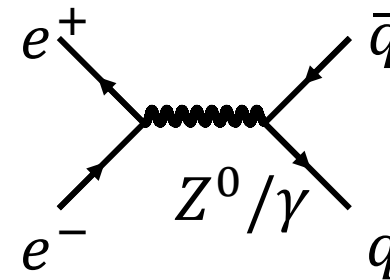
- The nominal selection cut is  $E_{\text{sum}}^{\text{hybrid}} > 83 \text{ GeV}$  with a purity of 99% with both leading and subleading jet in the acceptance
- A correction on the hybrid total energy selection is later applied to the unfolded leading dijet spectrum.



# Leading Dijet Spectrum vs. Generators

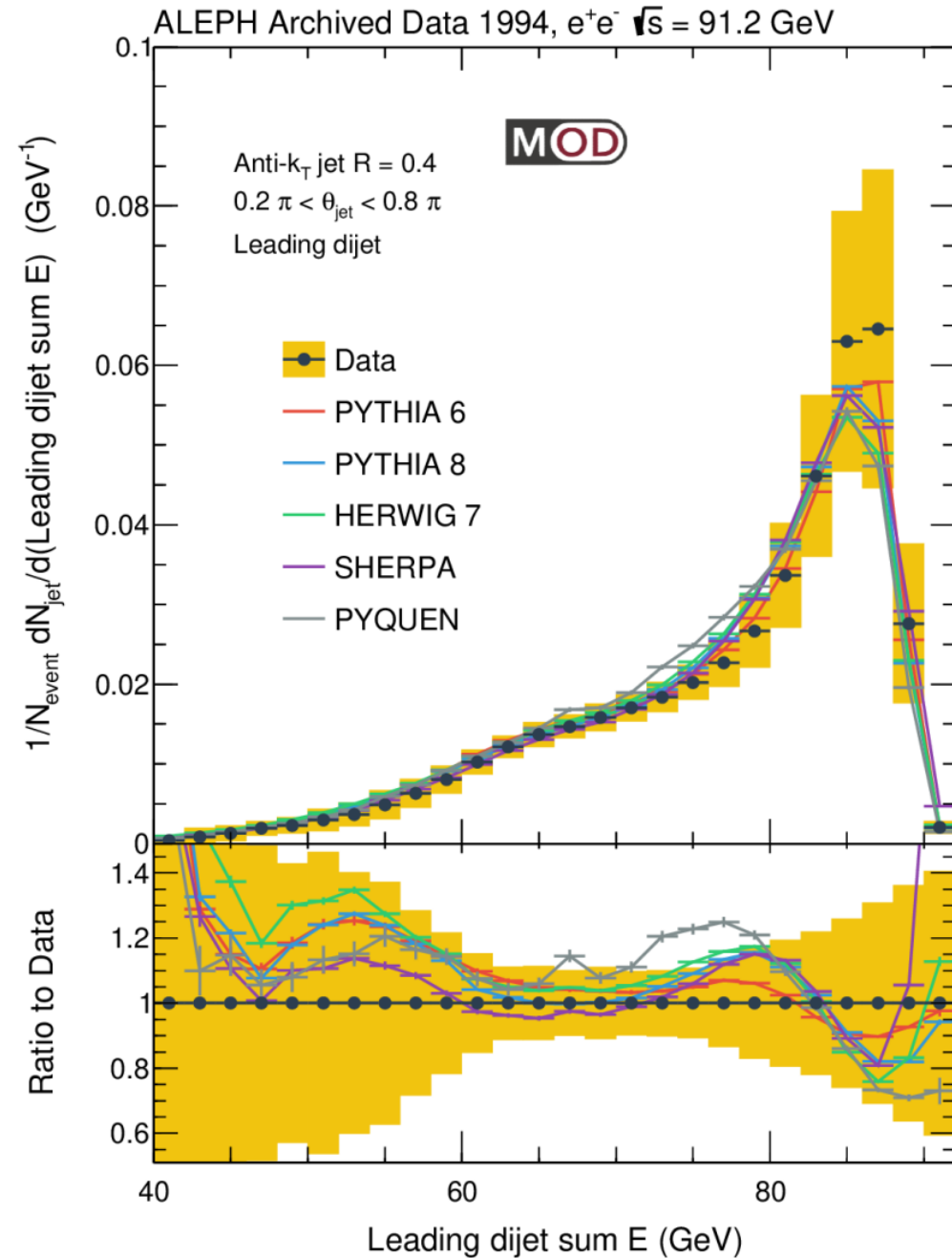


- Leading dijet energy spectrum: only include leading and subleading jets in the event (exclude other jets in the plot)
- Suppress jets from soft emissions and combinatorial jets
- A measurement of “energy loss” of (anti-)quark out of the jet cone due to parton shower
- Next-to-leading logarithmic (NLL') threshold and jet radius resummation gives a reasonable description of data

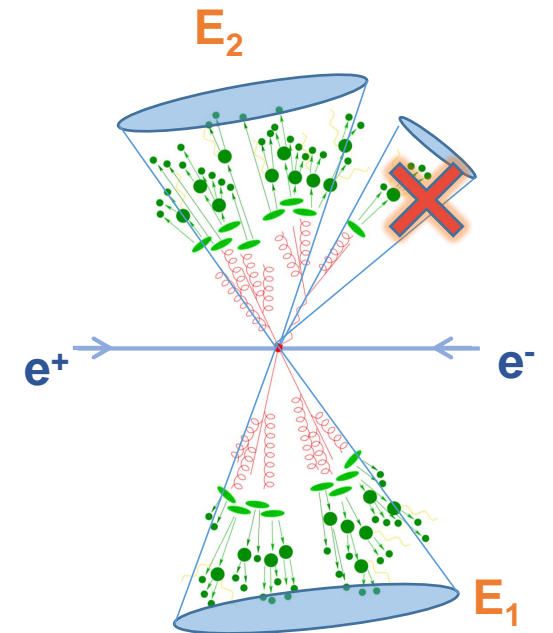
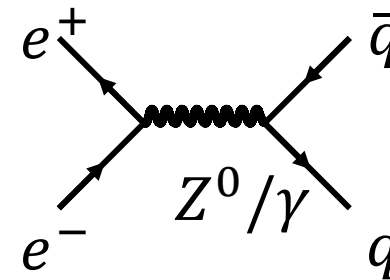


**\*\*NLL'+R calculation from Duff Neill, Felix Ringer, Nobuo Sato**

# Leading Dijet Energy Spectrum



- Sum of leading dijet energy (**sum  $E = E_1 + E_2$** )
- Suppress jets from soft emissions and combinatorial jets
- A measurement of “energy loss” of (anti-)quark out of the jet cone due to parton shower
- Generators capture general features of **data**



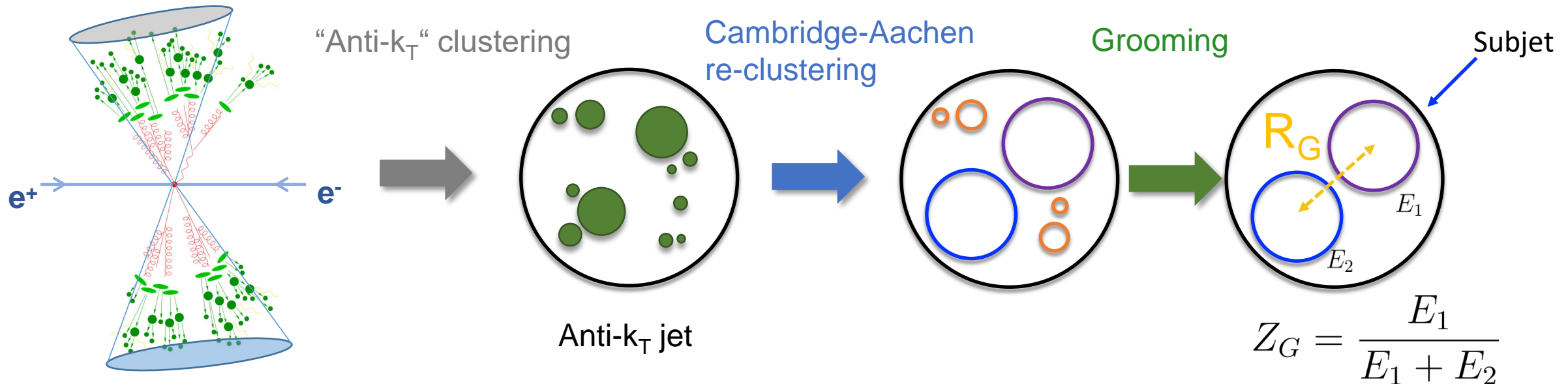
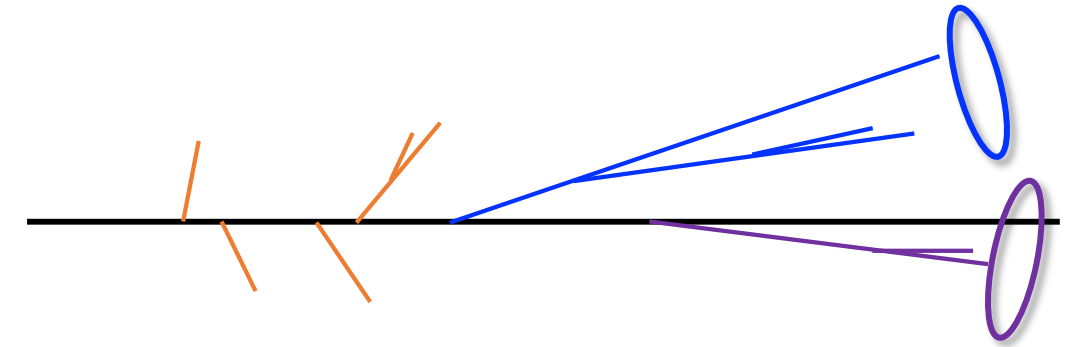


# Groomed Jet Substructure with Soft Drop

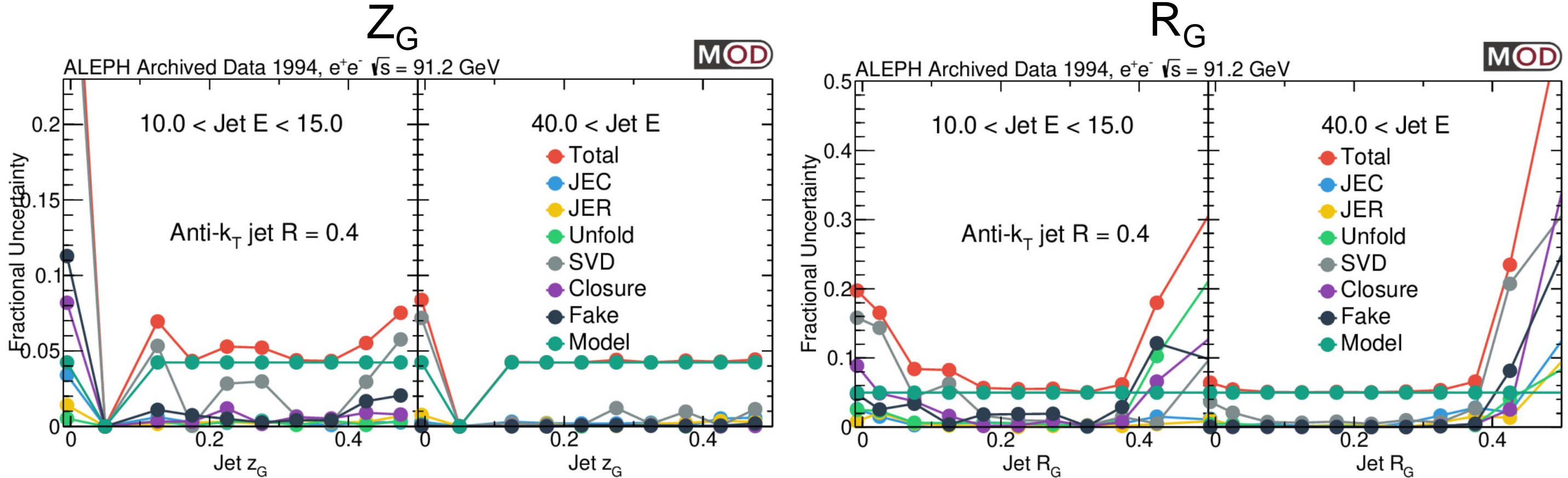
- Jet grooming: design observables **sensitive to different phase space**
  - Re-clustering with Cambridge-Aachen algorithm and grooming with a soft drop algorithm:

$$z \equiv \frac{\min(E_1, E_2)}{E_1 + E_2} \geq z_{\text{cut}} \left( \frac{\theta_{12}}{R_0} \right)^\beta$$

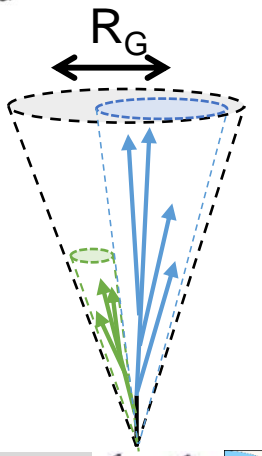
- $\theta_{12}$  is the **actual opening angle** between 1<sup>st</sup> and 2<sup>nd</sup> subjects
- Soft drop setting:  $Z_{\text{cut}}=0.1$  and  $\beta=0$ , identical to what are used in CMS pp and PbPb analyses
- $\beta=0 \rightarrow$  grooming independent of  $\theta$



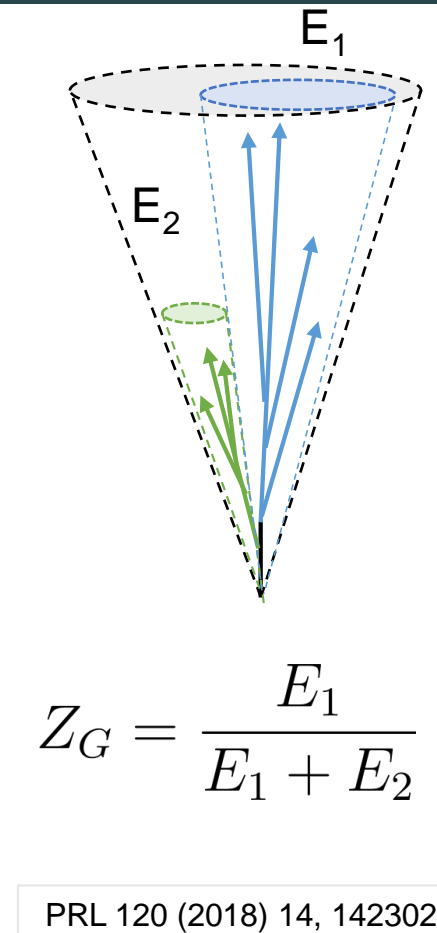
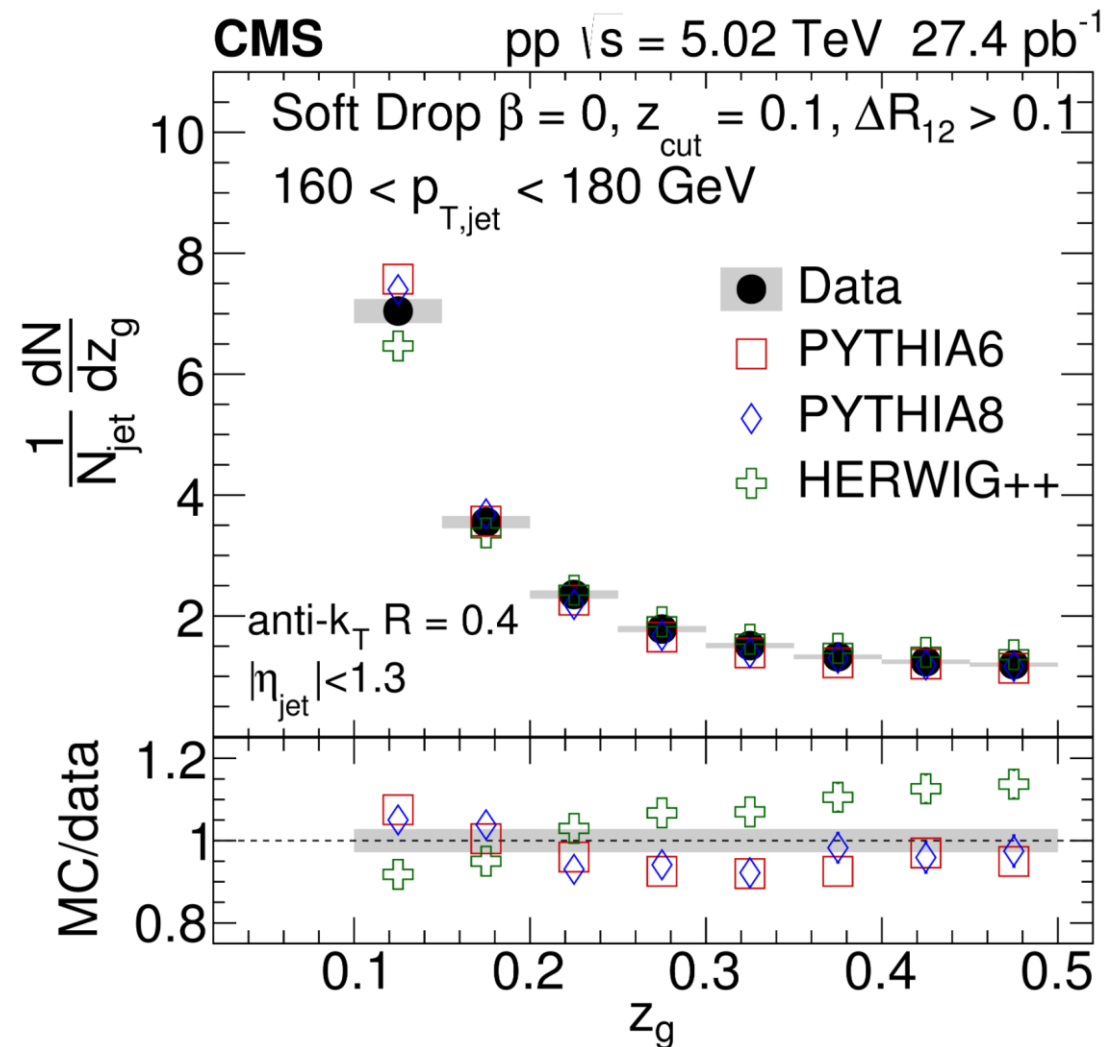
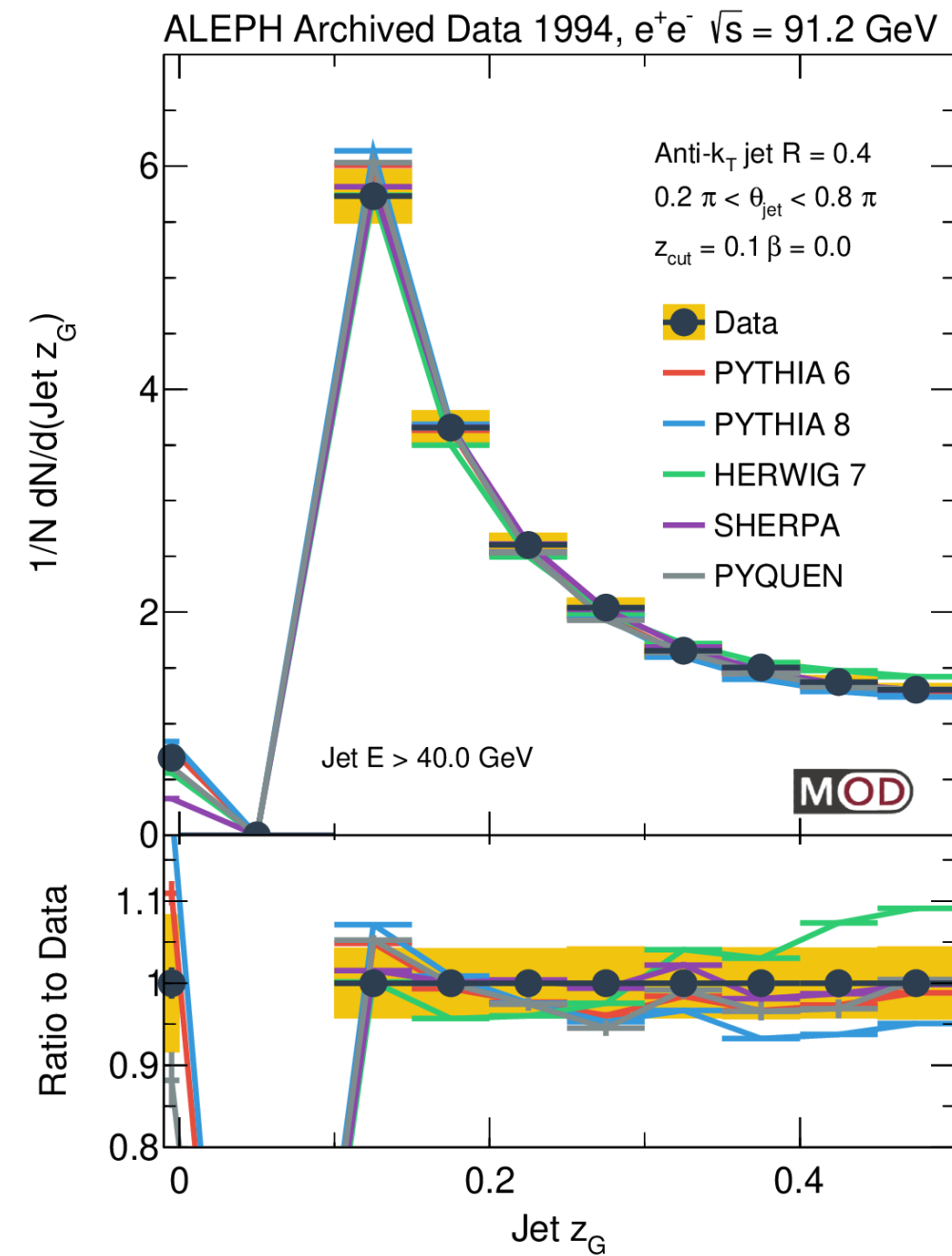
# Systematics: Jet Substructure



- Main uncertainty: Model dependence
  - Compare unfolded data with nominal and reweighted MC
  - Smear the subjet energy (3% on leading subjet and 6% on subleading subjet)
  - Smear the angle of subjets (by 0.002)



# Groomed Momentum Sharing $Z_G$

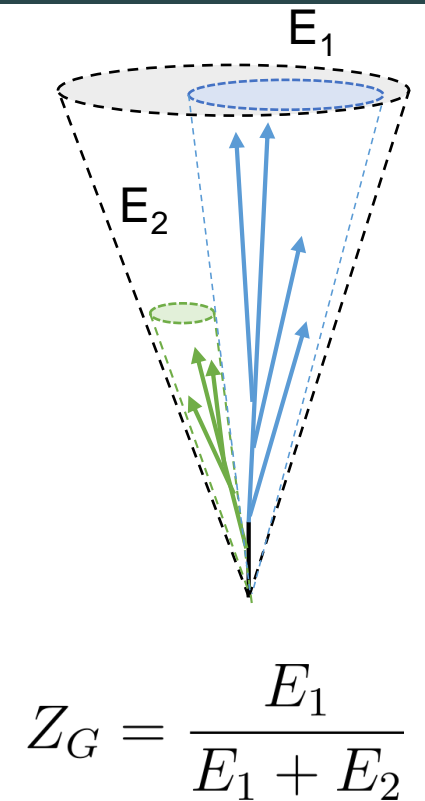
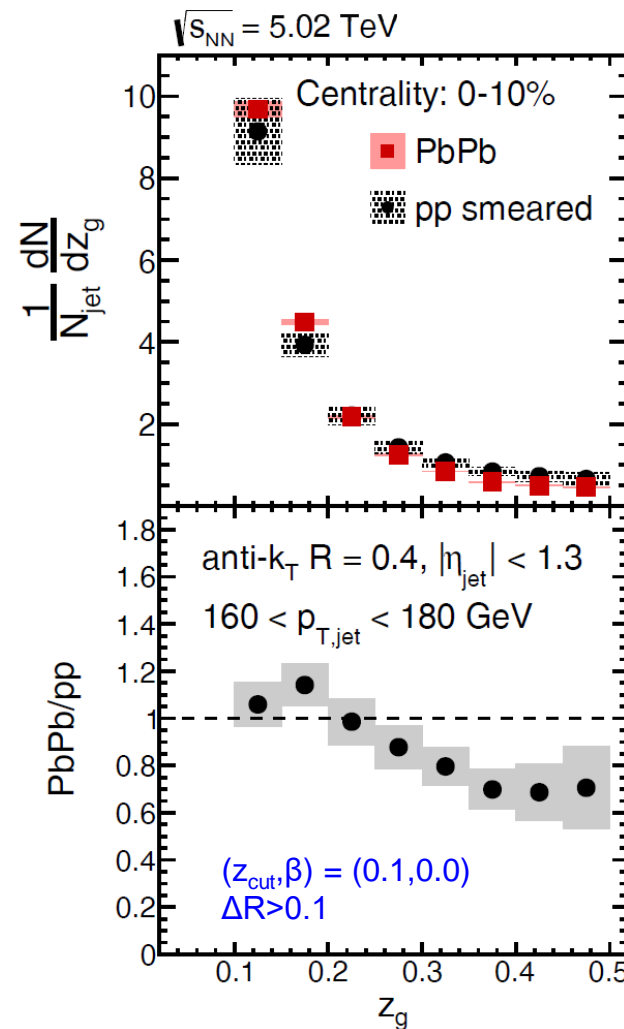
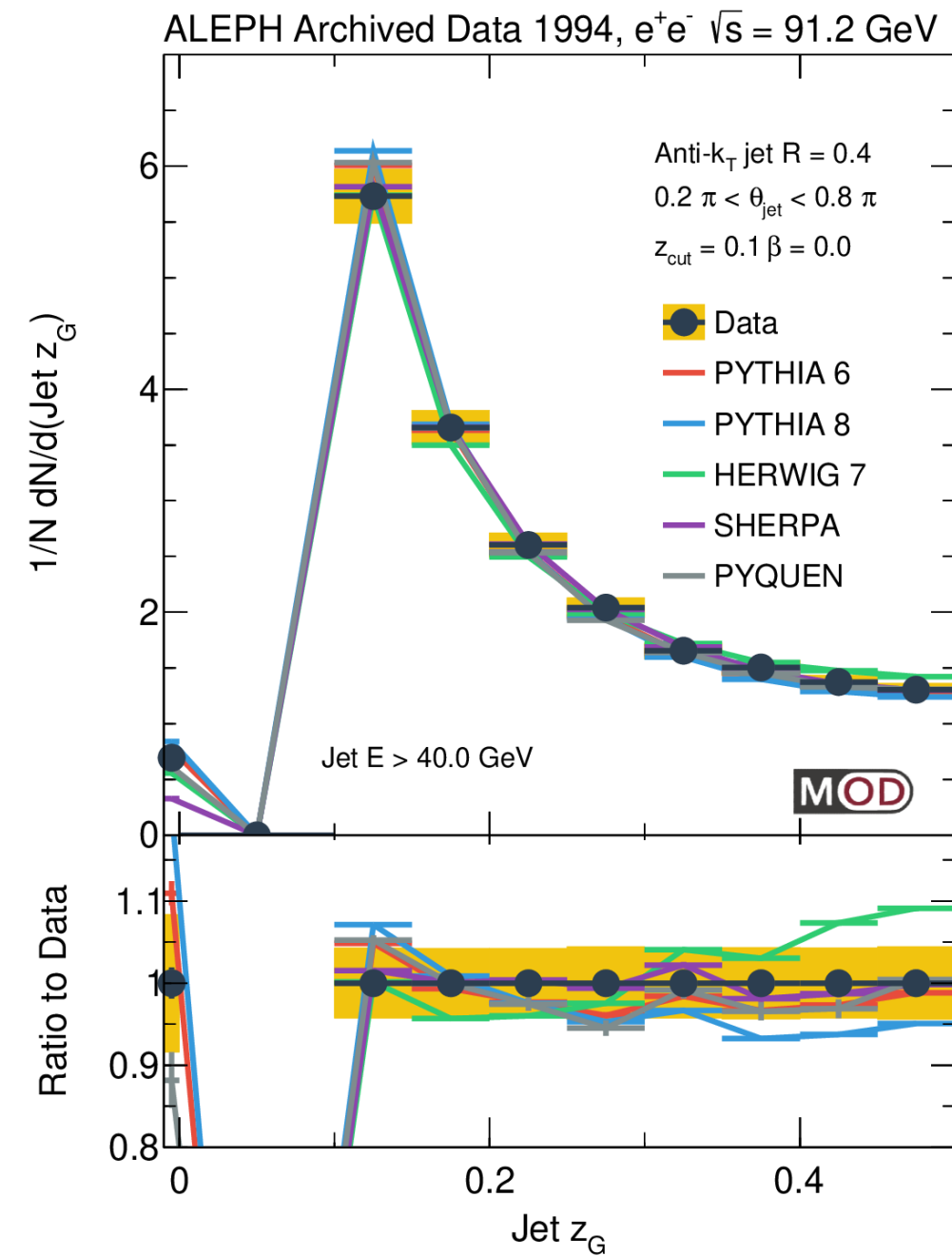


- At high jet energy, data wider than **PYTHIA 8**, narrower than **HERWIG**
- **Similar to the conclusion from pp data**

MITHIG-MOD-21-001  
[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
 JHEP 06 (2022) 008



# Groomed Momentum Sharing $Z_G$

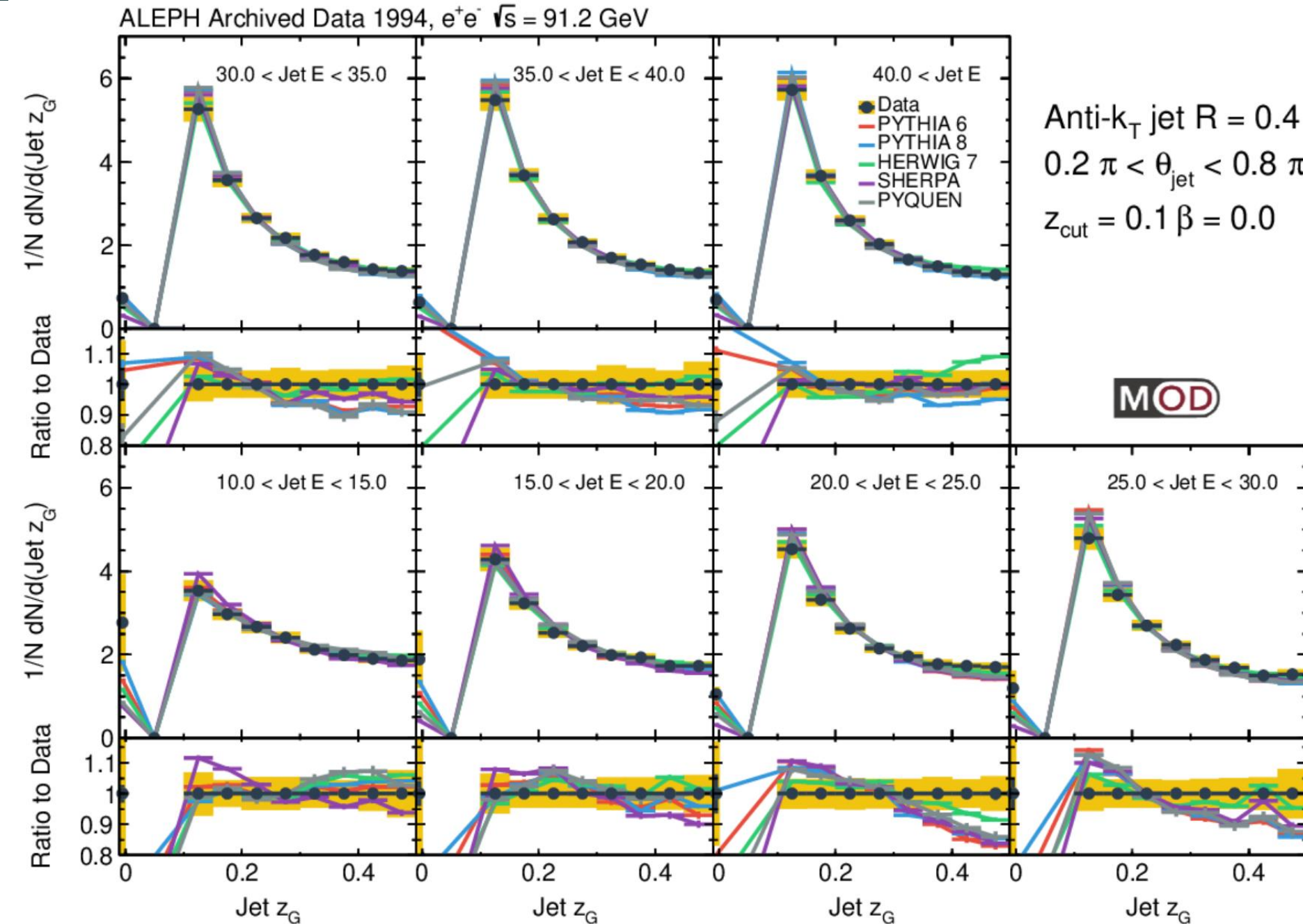


PRL 120 (2018) 14, 142302

MITHIG-MOD-21-001  
[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
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- In PbPb collisions, modification of  $Z_g$  for jets with  $R_g > 0.1$
- Size of the medium effect  $\sim$  discrepancy between pp (ee) data and event generators

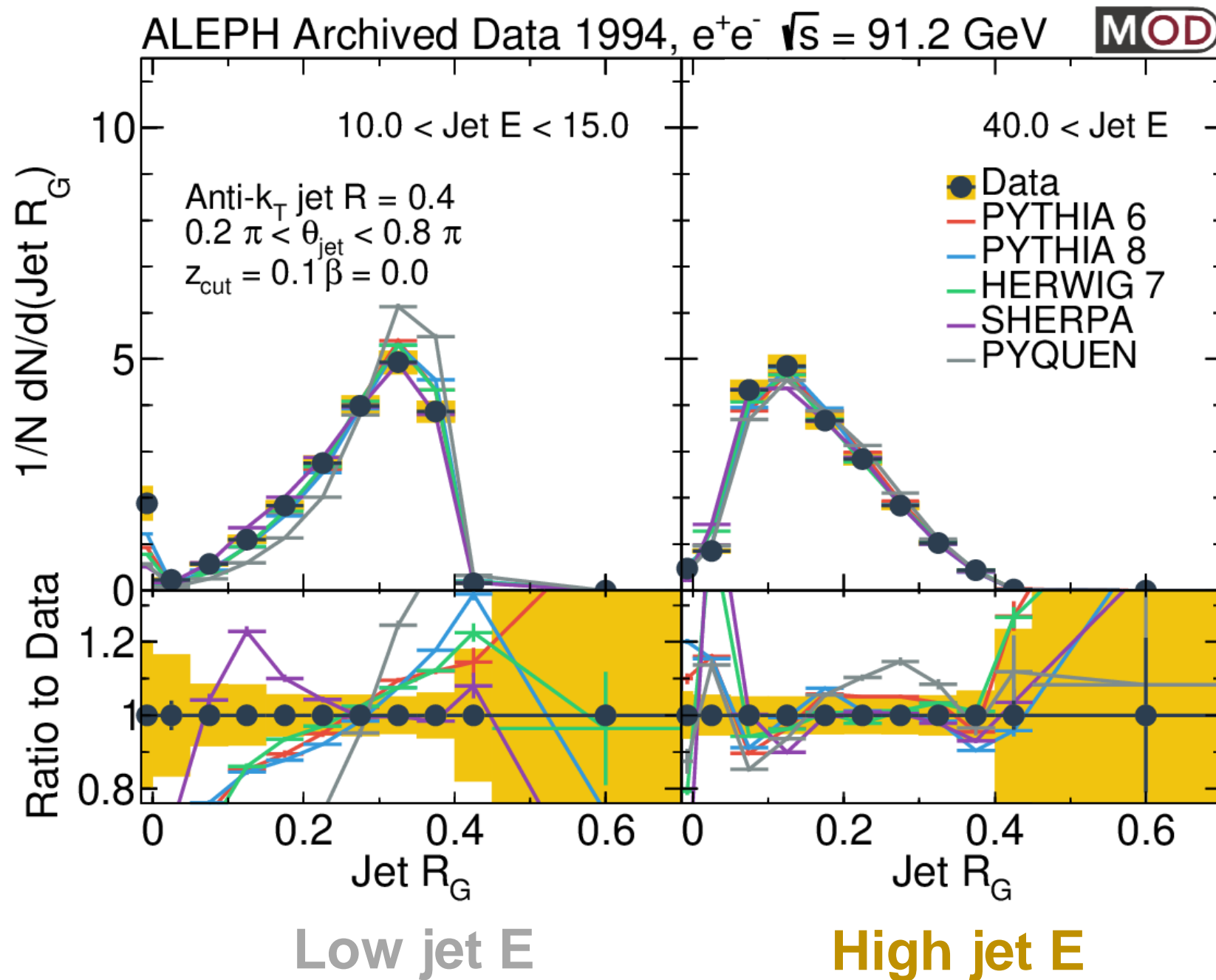
# Groomed Momentum Sharing $Z_G$ vs Jet E



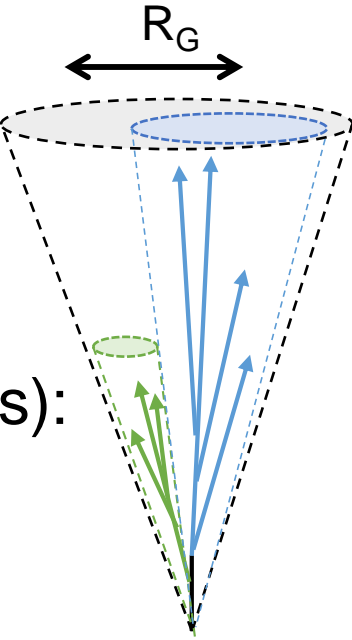
- The results are compared to **SHERPA**, **PYTHIA 6**, **PYTHIA 8**, **HERWIG**, and **PYQUEN**
- Most of the event generators describe the general trend (wider  $Z_G$  spectra as we go to lower E)
- None of the event generators provide full description of data (discrepancy up to around 15%)

MITHIG-MOD-21-001  
[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
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# Groomed Jet Radius $R_G$ vs. Event Generators



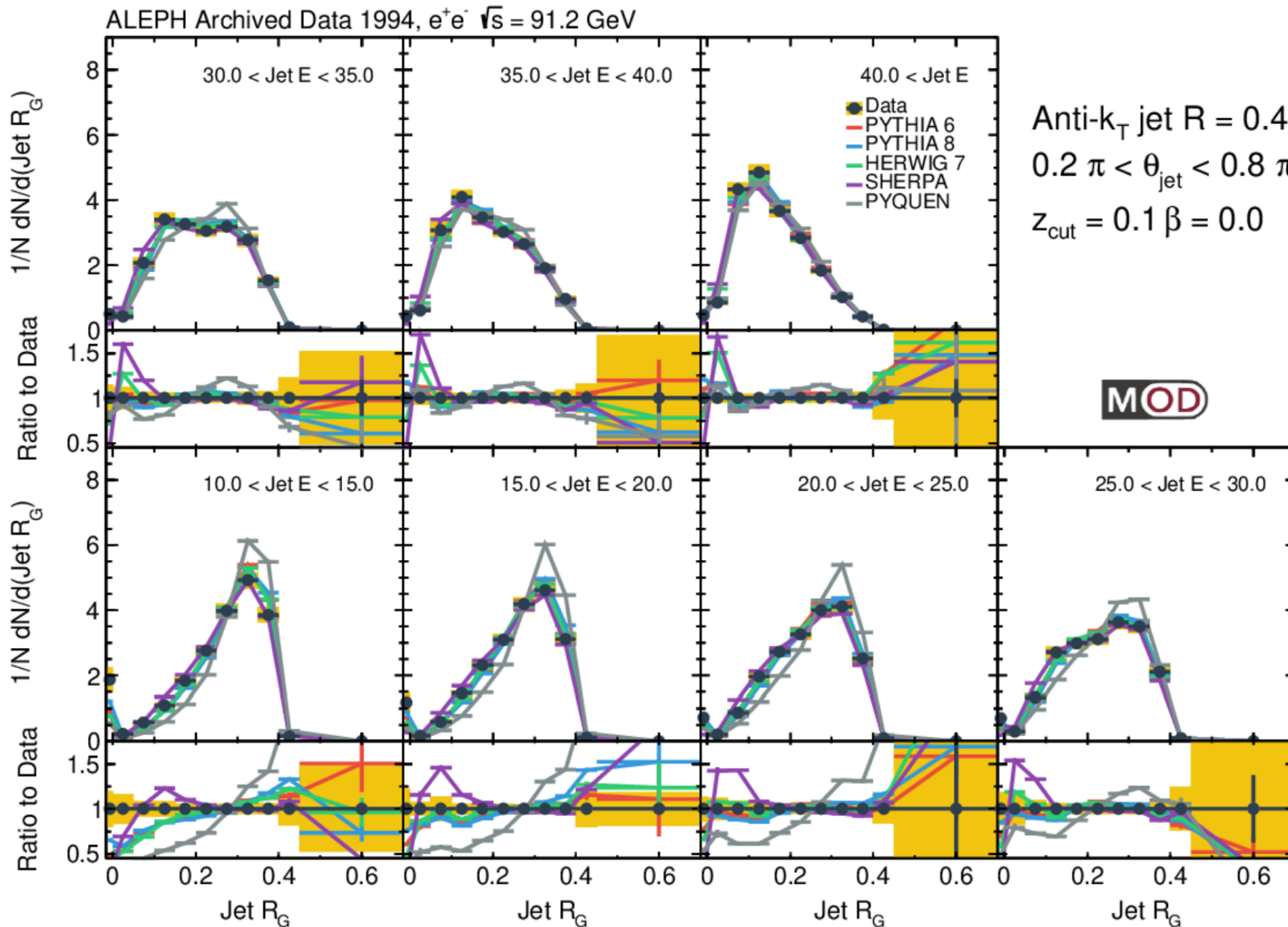
MITHIG-MOD-21-001  
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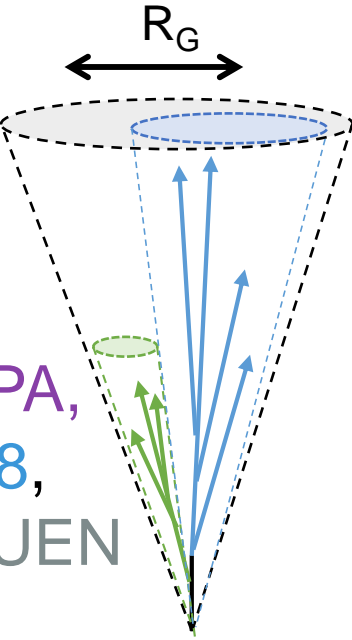
- **High jet E** (mainly quark jets):
  - Peak at smaller  $R_G$  value
  - Generators give a better description of the data
- **Low jet E** (mainly from soft emissions and combinatorial):
  - Peak at larger  $R_G$  value as one would expect
  - **SHERPA** gives a better description of the data
  - **PYTHIA 6**, **PYTHIA 8**, **HERWIG**, and **PYQUEN** overpredict the  $R_G$



# Groomed Jet Radius $R_G$ vs. Event Generators

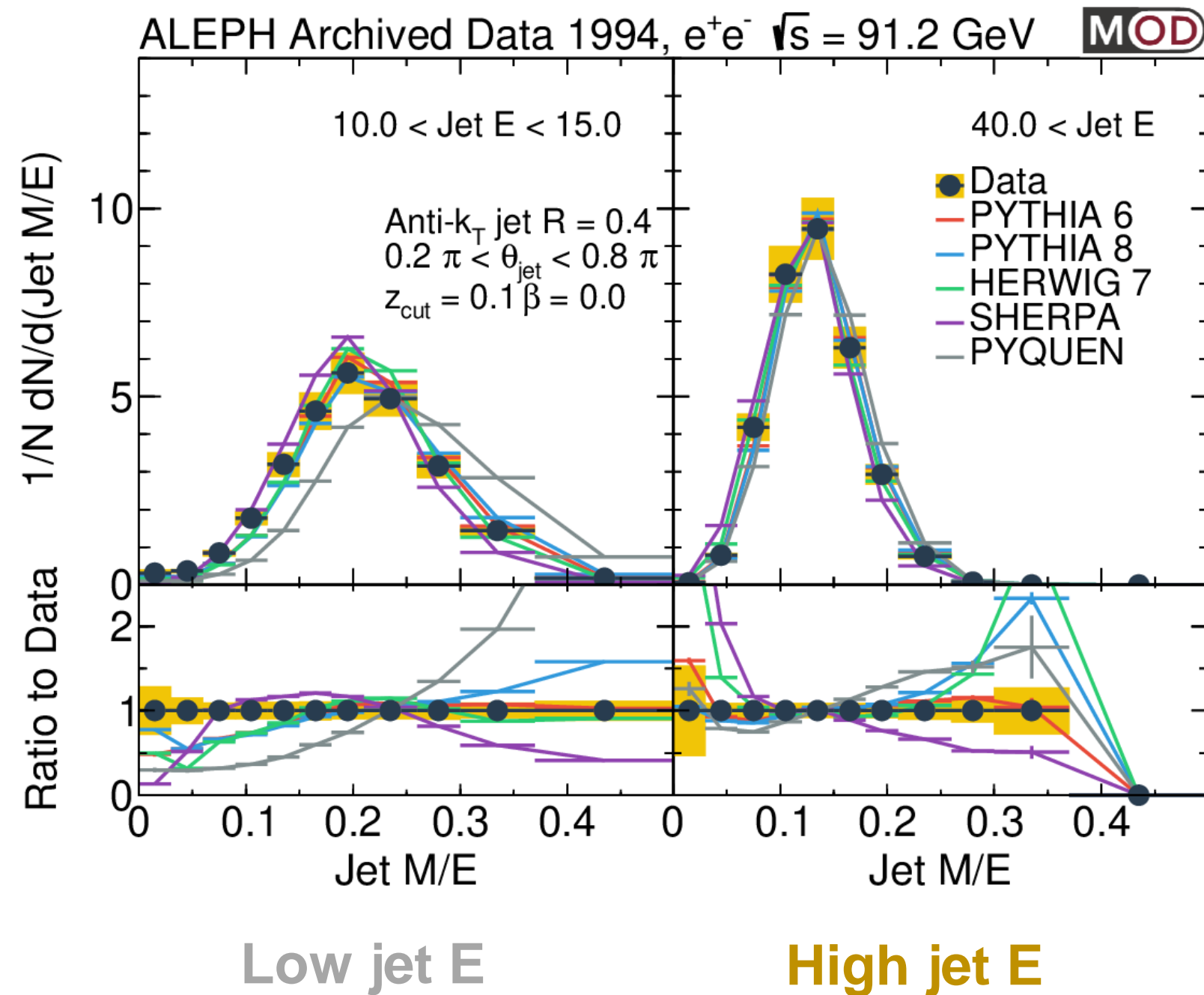


MITHIG-MOD-21-001  
[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
 JHEP 06 (2022) 008



- The results are compared to **SHERPA**, **PYTHIA 6**, **PYTHIA 8**, **HERWIG**, and **PYQUEN**
- Groomed jet radius decreases as a function of jet energy
- Archived **PYTHIA 6.1** is closer to the data
- None of the event generators provide full description of data (discrepancy up to ~50%)

# Jet Mass / Energy Ratio

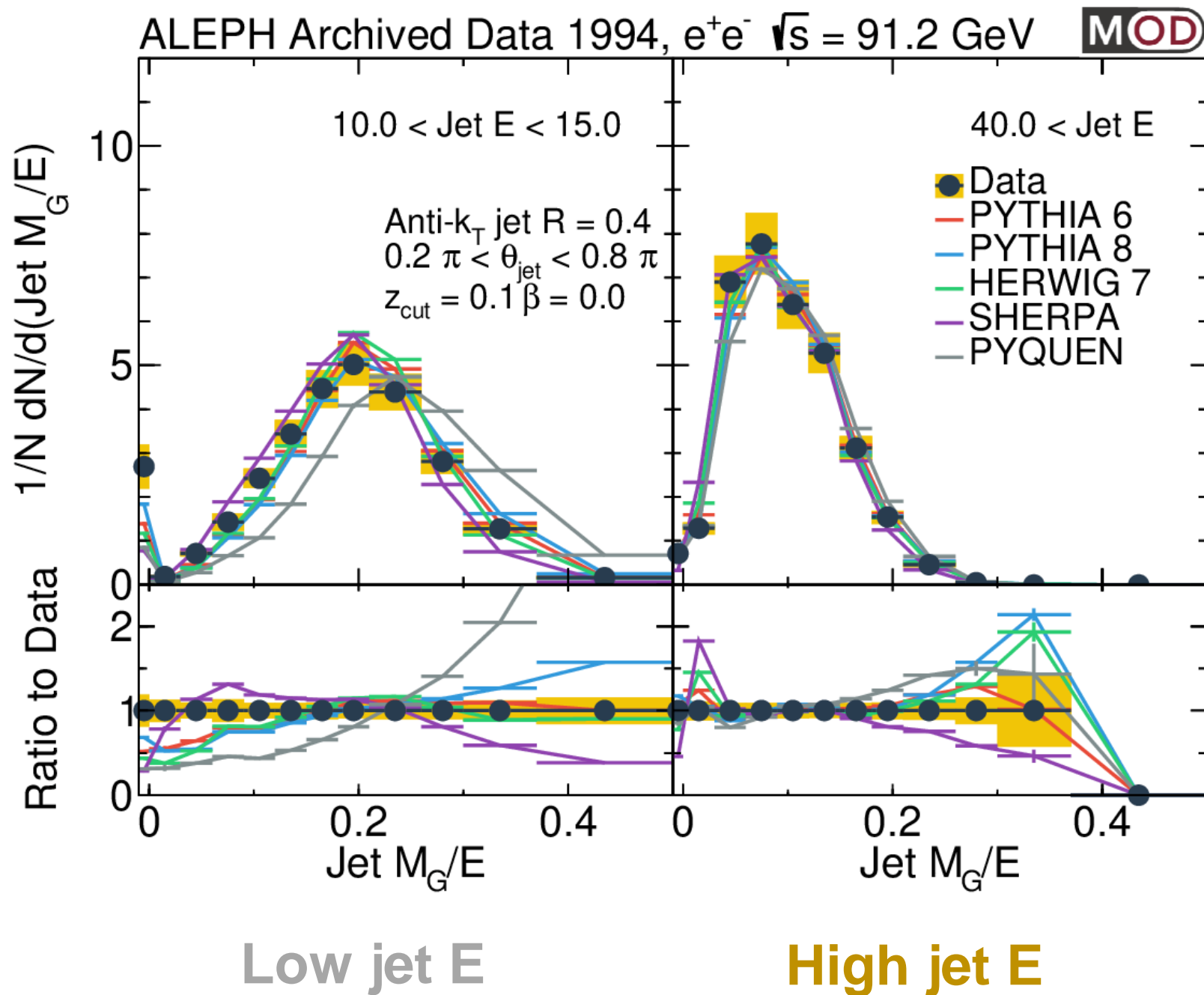


## Jet M/E:

- SHERPA, PYTHIA 8, HERWIG, and PYQUEN don't describe the distribution well.
- Archived **PYTHIA 6.1** is closer to the data
- SHERPA: lower mass than other generators

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# Groomed Jet Mass / Energy Ratio



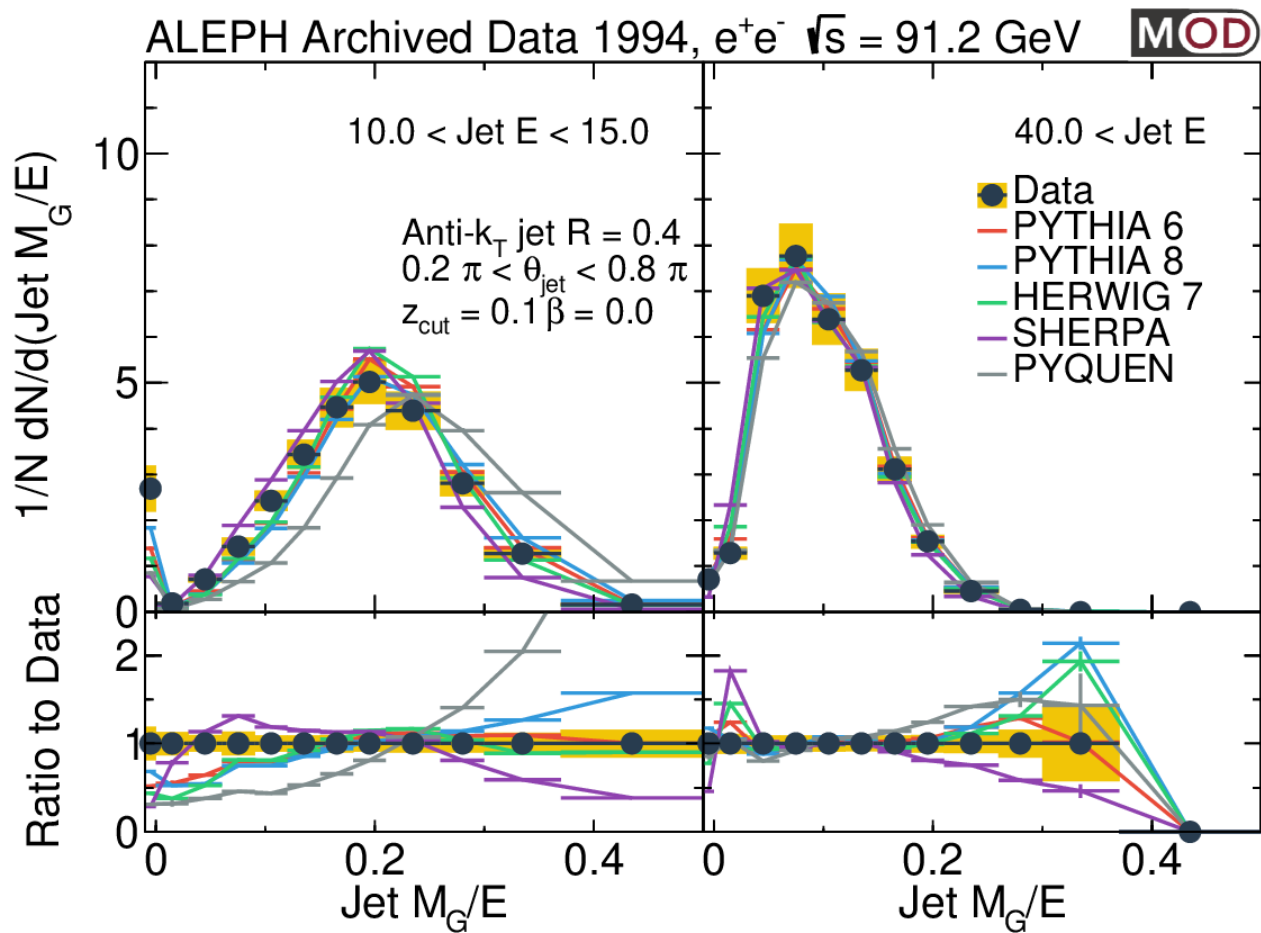
## Groomed Jet $M_G/E$ :

- Reduce the impact of soft radiation in the jet cone
- Jet mass becomes smaller after grooming
- Similar discrepancies seen between data and generators as the ungroomed mass
- To enhance the sensitivity to soft emissions: Follow up with  $(M-M_G)/E$  and collinear drop observables in the future

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[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
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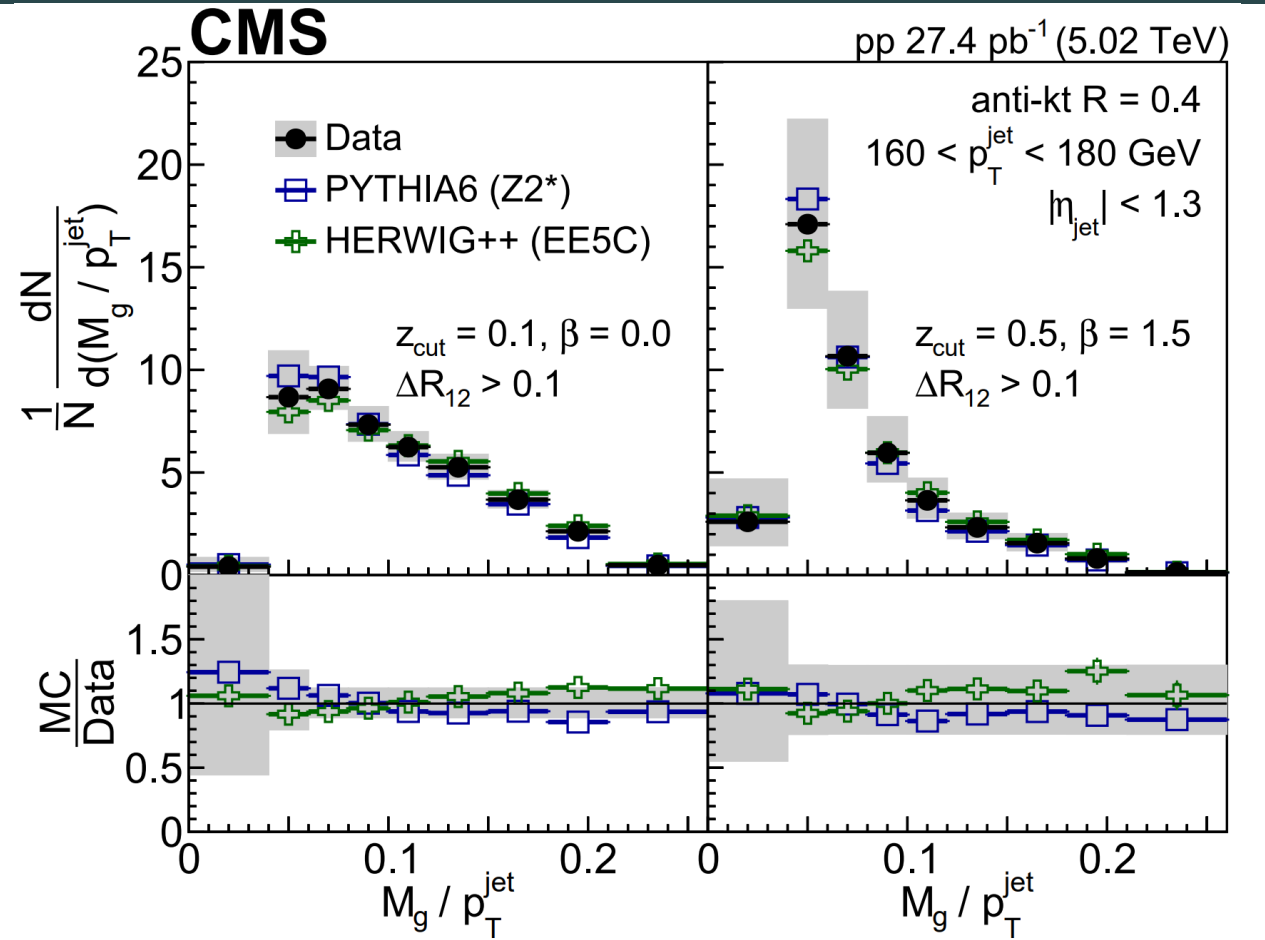


# Groomed Jet Mass in $e^+e^-$ and pp



MITHIG-MOD-21-001  
[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
 JHEP 06 (2022) 008

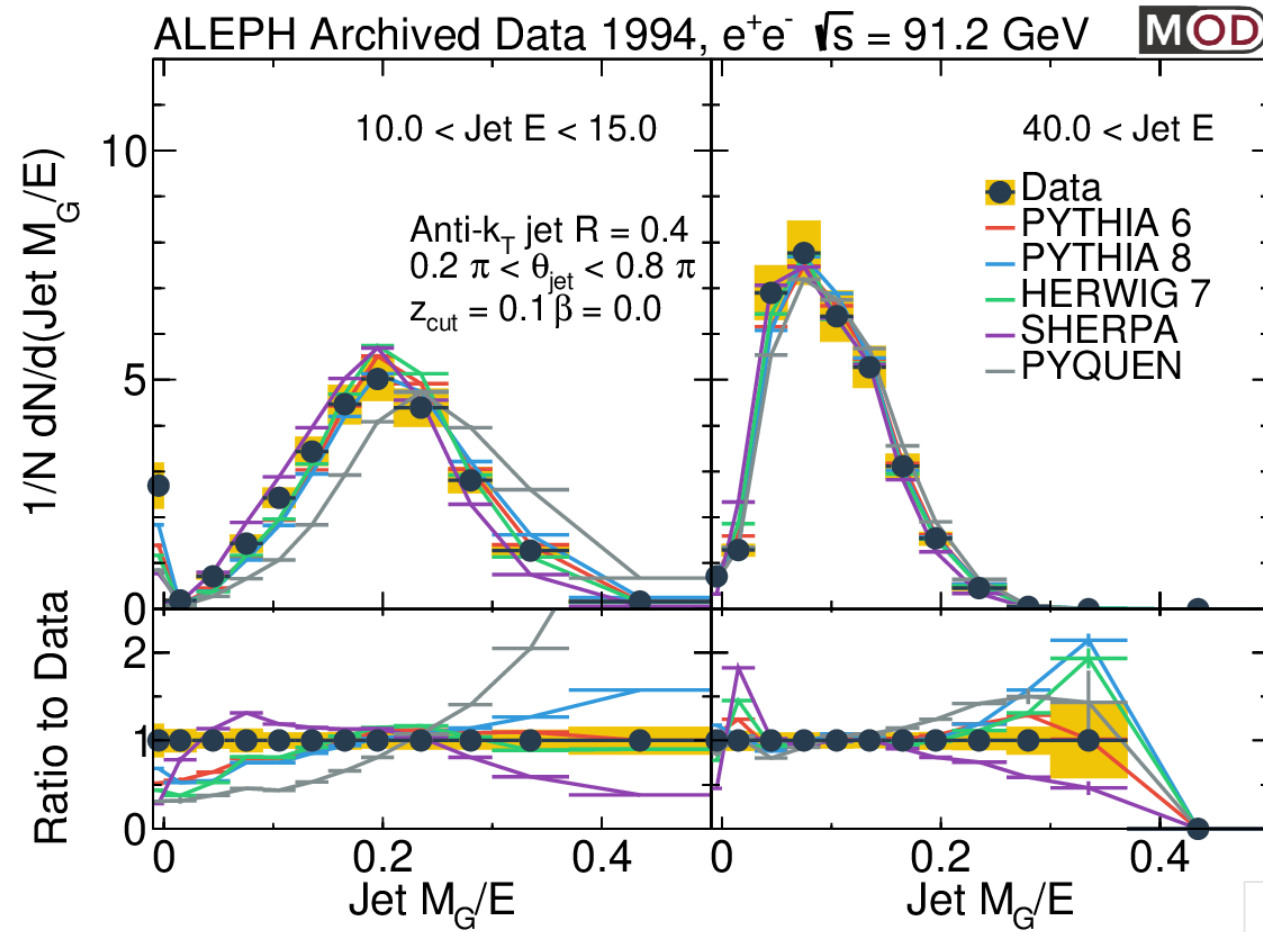
- Large difference between  $e^+e^-$  data and event generators



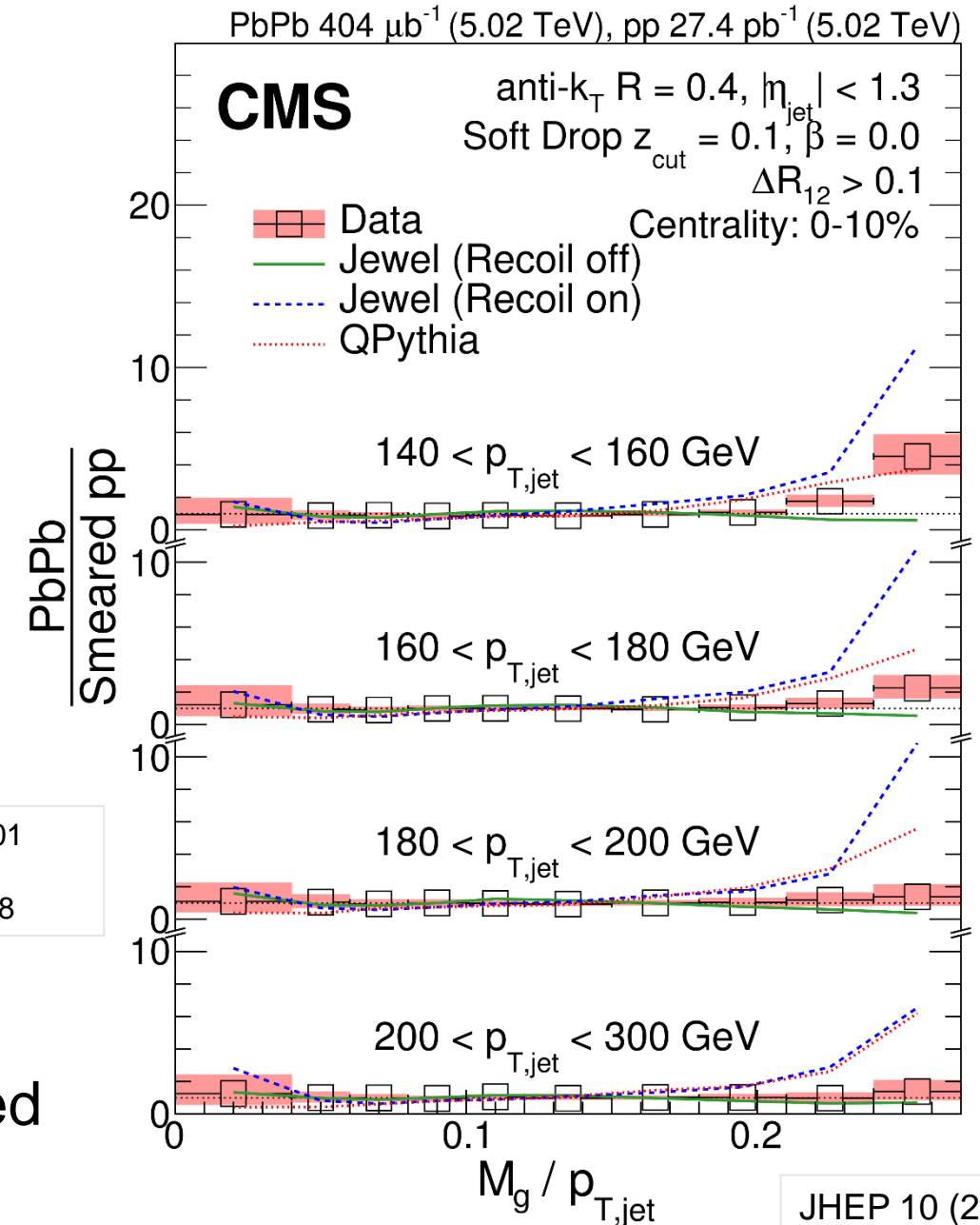
JHEP 10 (2018) 161

- Within the experimental uncertainties, event generators agree with pp data
- Cancellation of effects from MPI and shower?

# Groomed Jet Mass in $e^+e^-$ and PbPb



MITHIG-MOD-21-001  
[arXiv:2111.09914](https://arxiv.org/abs/2111.09914)  
 JHEP 06 (2022) 008

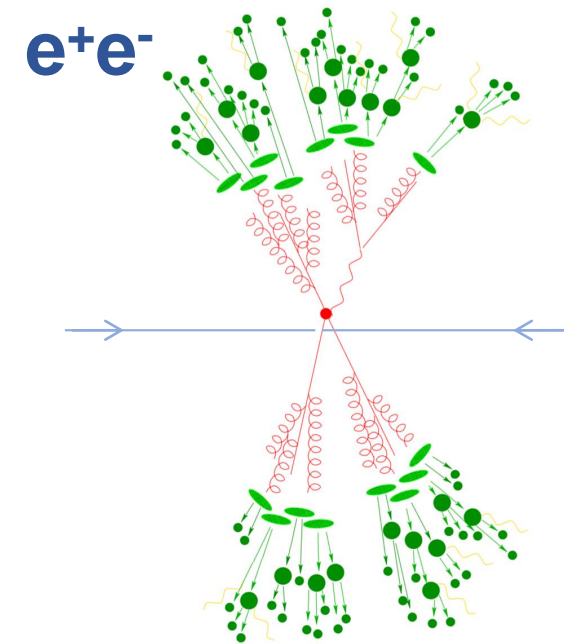


JHEP 10 (2018) 161

- PbPb: modification mass spectra
  - In particular, at high and low  $M_g/p_T$  regions
- Also the phase space where  $e^+e^-$  data is poorly described by event generators

# From $e^+e^-$ to EIC

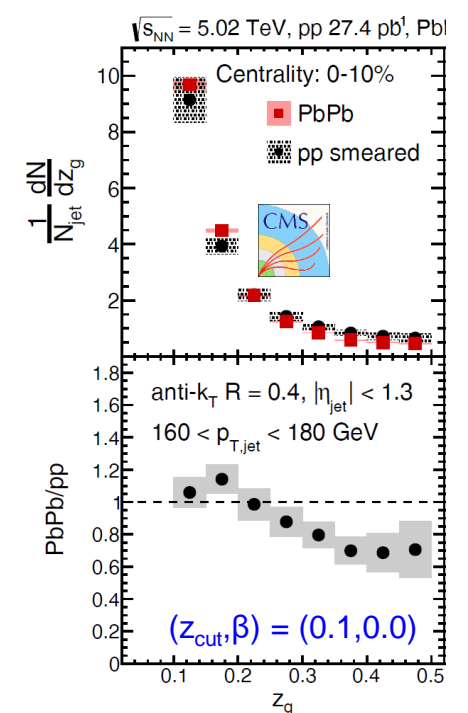
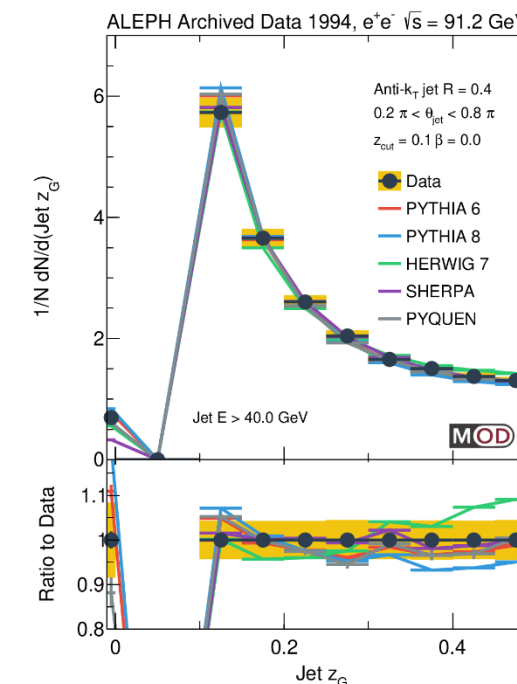
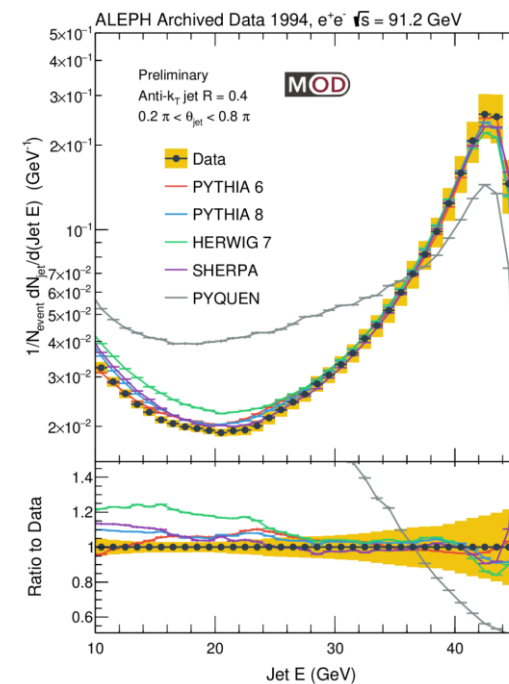
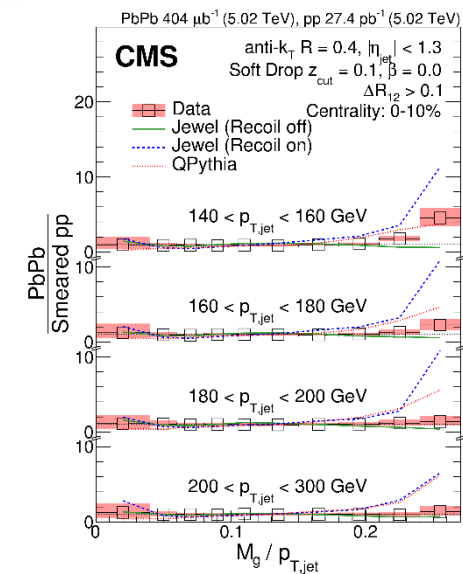
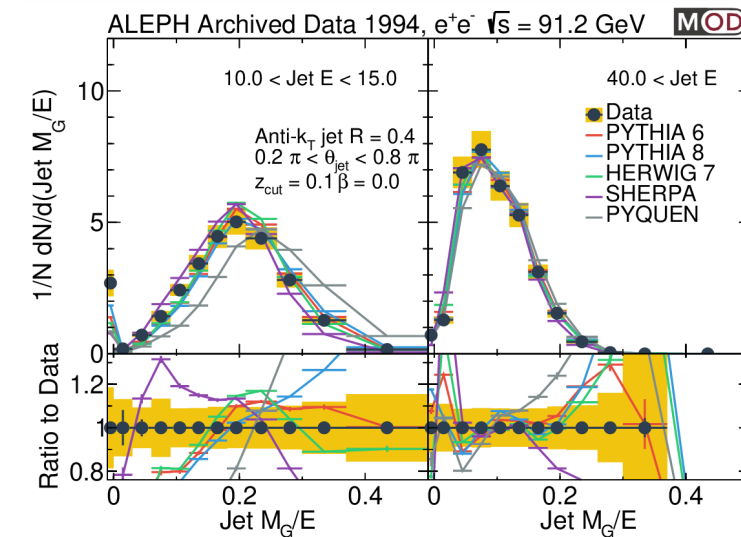
- $e^+e^-$  jet data provide opportunities to validate theoretical approaches and tuning of event generator
  - High accuracy pQCD calculations
  - Hadronization
- Provide tests on EIC-inspired jet algorithms
  - For instance, Centauro
- Provide tests on the new observables
  - Such as EC and CF
- Reference for ep and eA data at EIC





# Summary

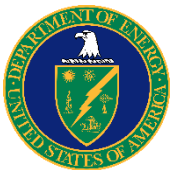
- The first measurement of anti- $k_T$  jet energy spectra and substructure in hadronic  $e^+e^-$  collisions
- None of the event generators gives full description of the  $e^+e^-$  data (discrepancy as large as 10-50%)
- Discrepancy between data and generators in  $e^+e^-$  is as large as the difference between pp and PbPb in places
- Provide new inputs to event generators and hadronization models
- We look forward to more future analyses with this dataset such as:
  - Jet substructure vs. event multiplicity
  - Jet fragmentation function
  - Strangeness content
  - EIC jet algorithm and observables
 ... stay tuned!



# Acknowledgement

We would like to thank **Roberto Tenchini** and **Guenther Dissertori** from the ALEPH collaboration for the useful comments and suggestions on the use of ALEPH archived data.

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# Thank you!



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Austin Baty  
(Rice, CMS)



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(CU Boulder, ATLAS)



Michael Peters  
(MIT, CMS)



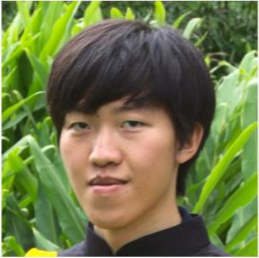
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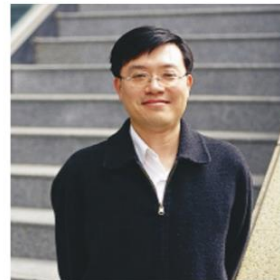
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Paoti Chang  
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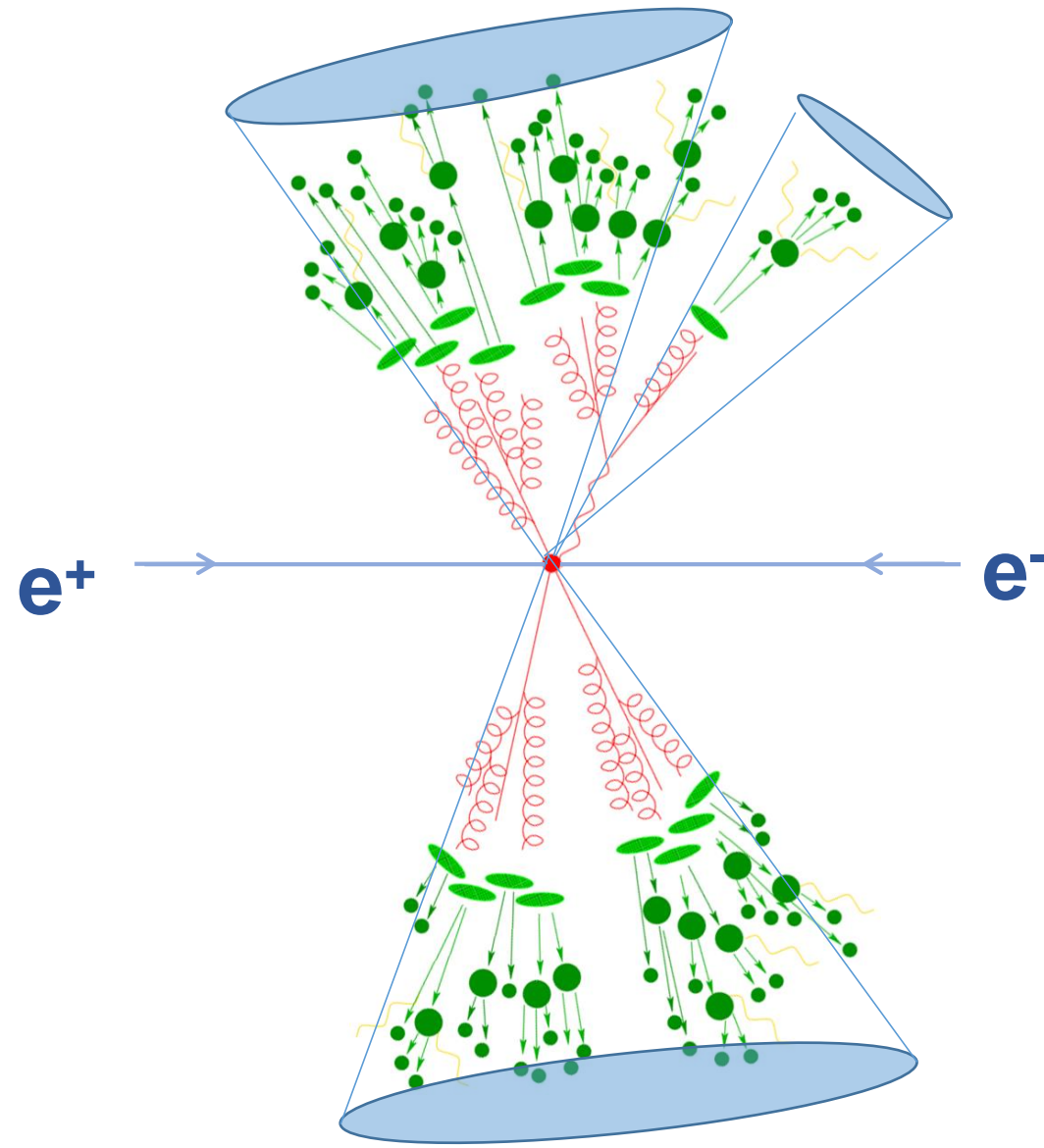
Marcello Maggi  
(INFN, CMS)



Günther Dissertori  
(ETH Zürich, CMS)



# Backup Slides



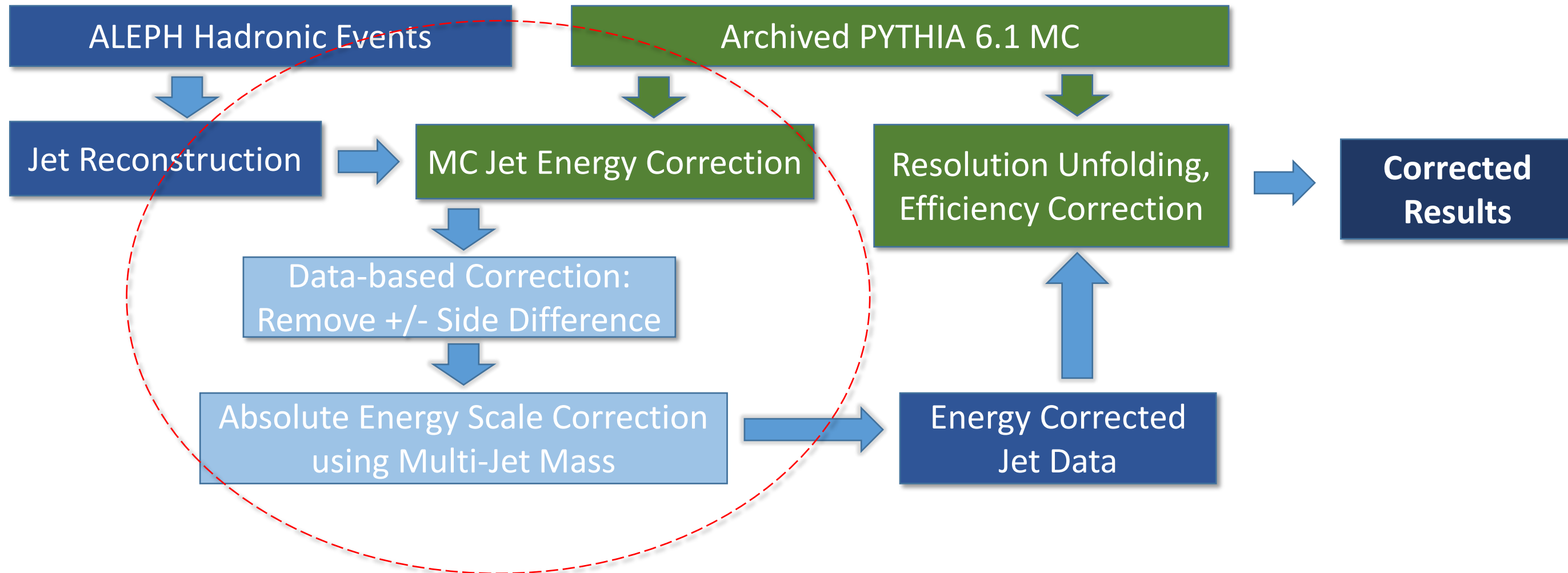
# $Z^0$ Hadronic Decay Event Selection

- **Track Selection:**
  - Particle Flow Candidate 0, 1, 2
  - Number of TPC hits for a charged tracks  $\geq 4$
  - $|d_0| < 2$  cm
  - $|z_0| < 10$  cm
  - $|\cos\theta| < 0.94$
  - $p_T > 0.2$  GeV (transverse momentum with respect to beam axis)
  - $N_{\text{TPC}} \geq 4$
  - $\chi^2/\text{ndf} < 1000$ .
- **Neutral Hadron Selection:**
  - Particle Flow Candidate 4, 5 (ECAL / HCAL object)
  - $E > 0.4$  GeV
  - $|\cos\theta| < 0.98$
- **Event Selection:**
  - Number of good charged particles  $\geq 5$  (including charged hadrons and leptons)
  - Number of good ch+neu. Particles  $\geq 13$
  - $E_{\text{charged}} > 15$  GeV
  - $|\cos(\theta_{\text{sphericity}})| < 0.82$

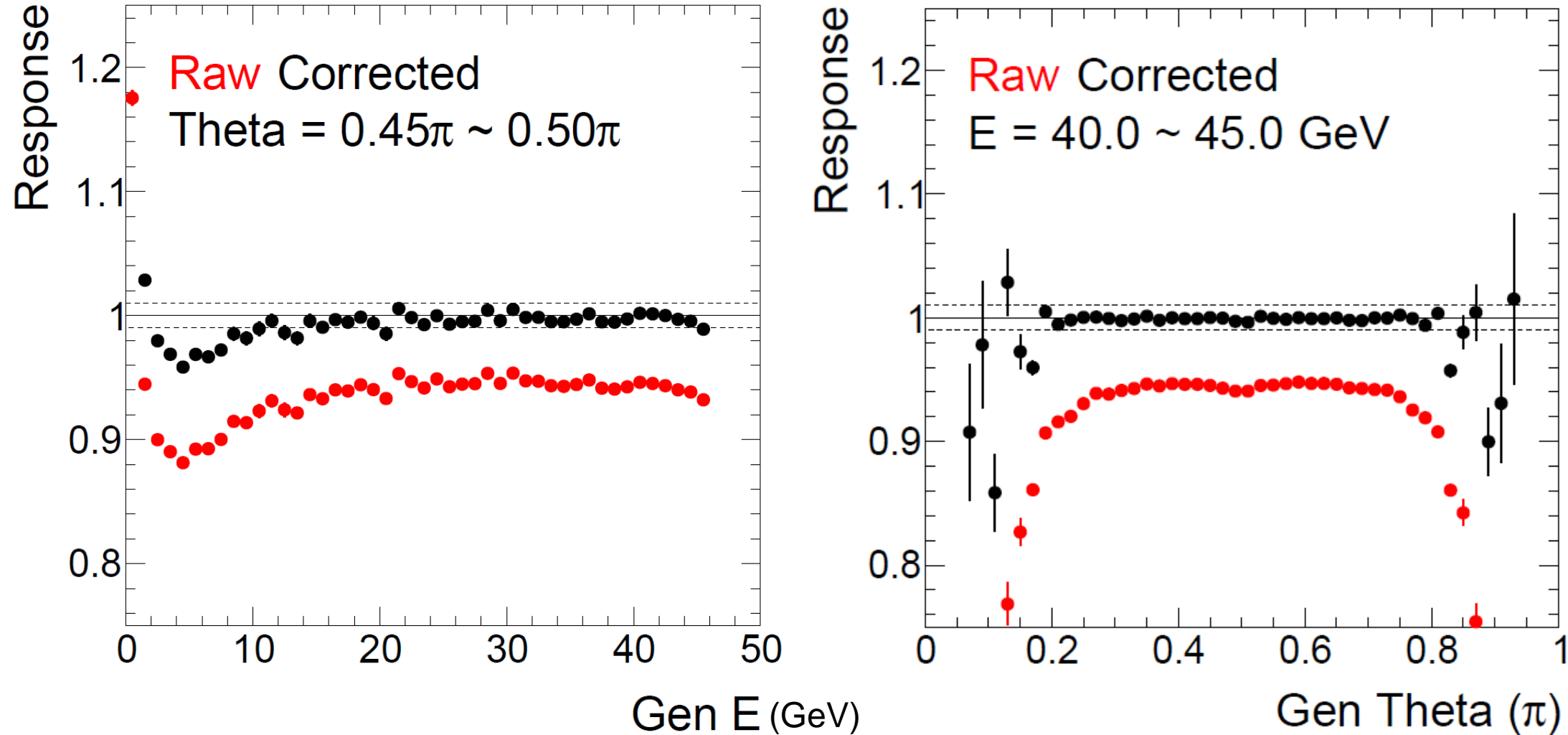
# Jet Energy Correction Steps

In order to inspect the event in a shower-by-shower basis, we need to perform jet reconstruction

Jet analysis workflow:



# MC Jet Energy Correction

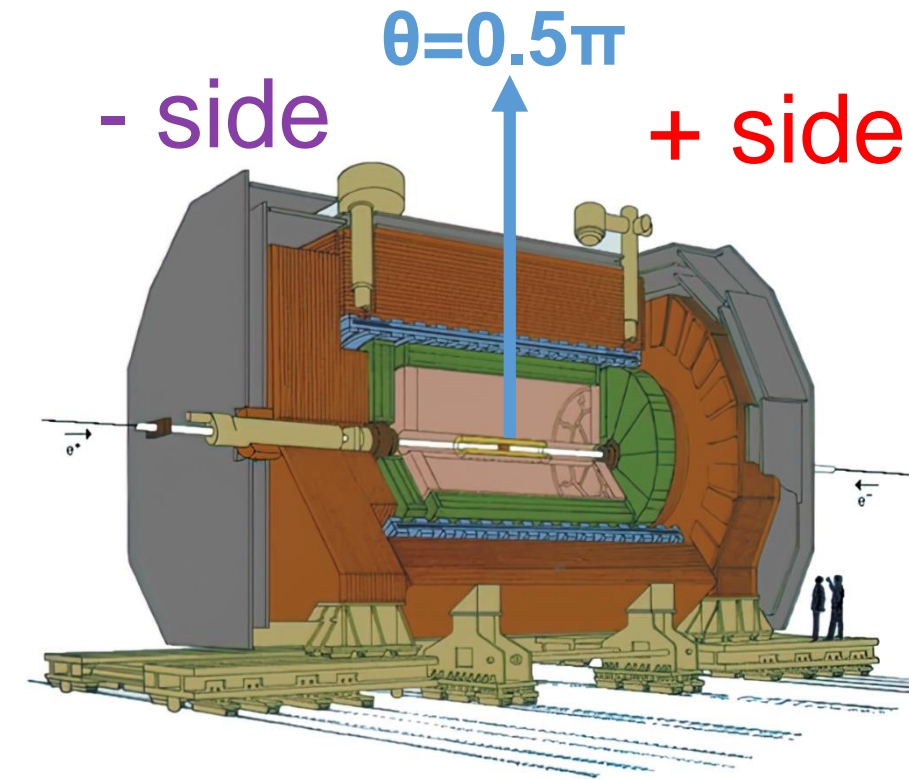
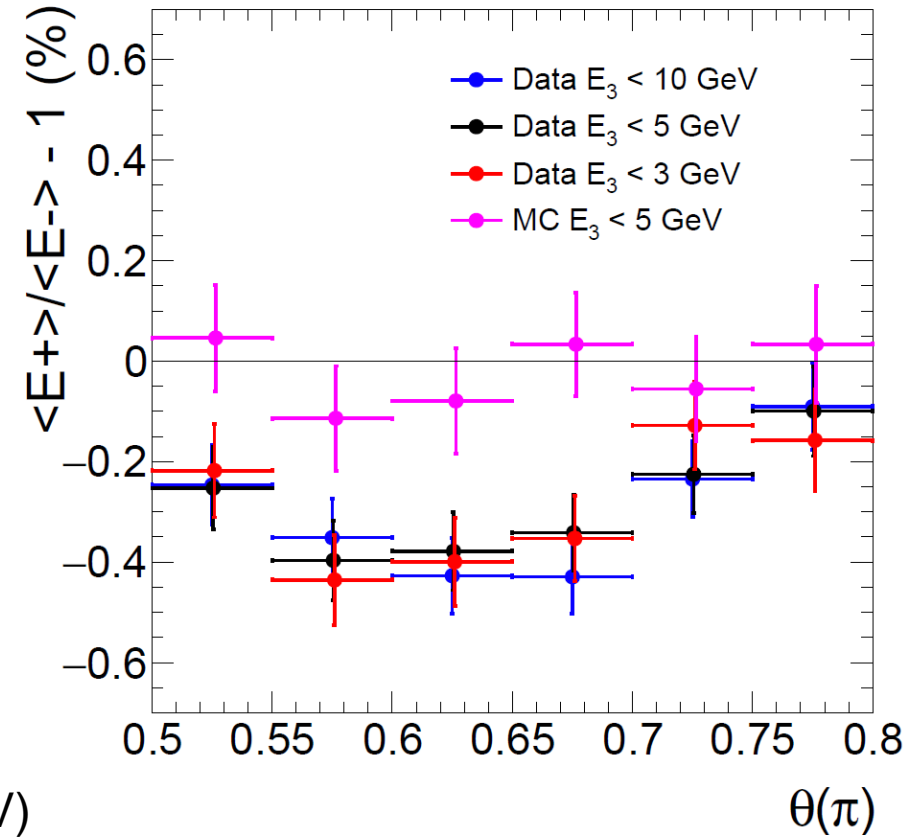
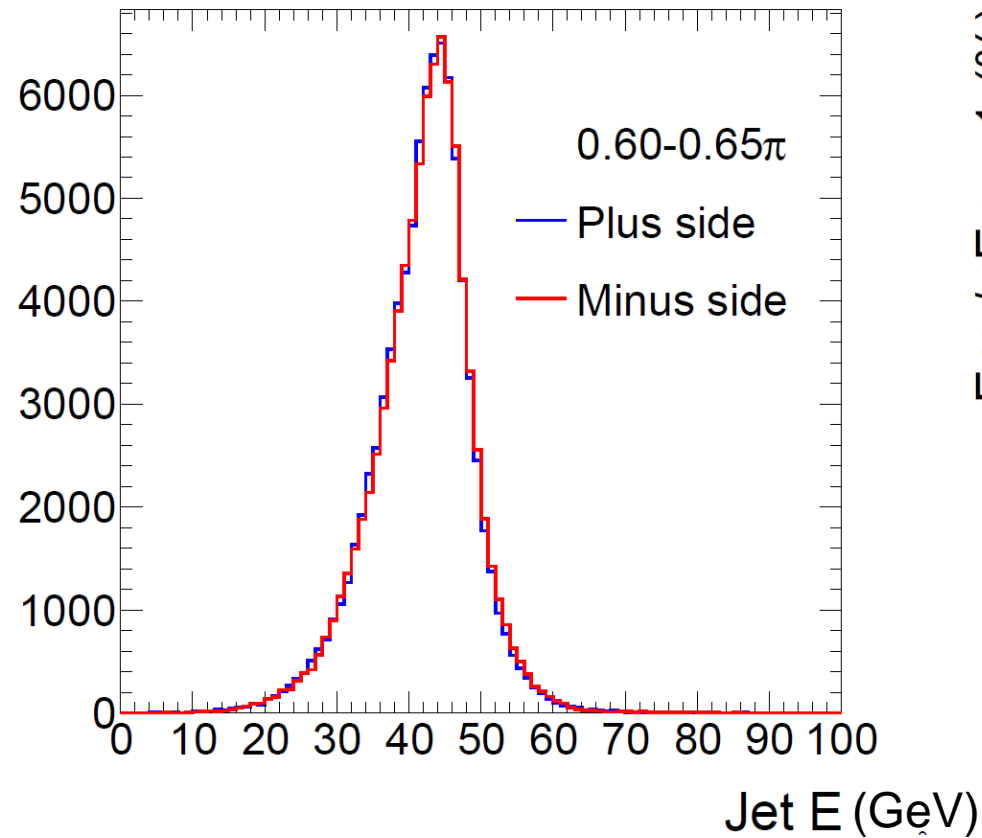


Yi Chen  
(MIT, CMS)

- **Archived PYTHIA 6.1 MC** (tuned to describe ALEPH hadron spectra) was used for jet energy calibration
- **Response** = (**Raw** or **Corrected**) Reconstructed jet energy / “Generated jet energy” in truth level
- Good closure was achieved for  **$E > 10 \text{ GeV}$**  and  **$0.2\pi < \text{Jet } \theta < 0.8\pi$**



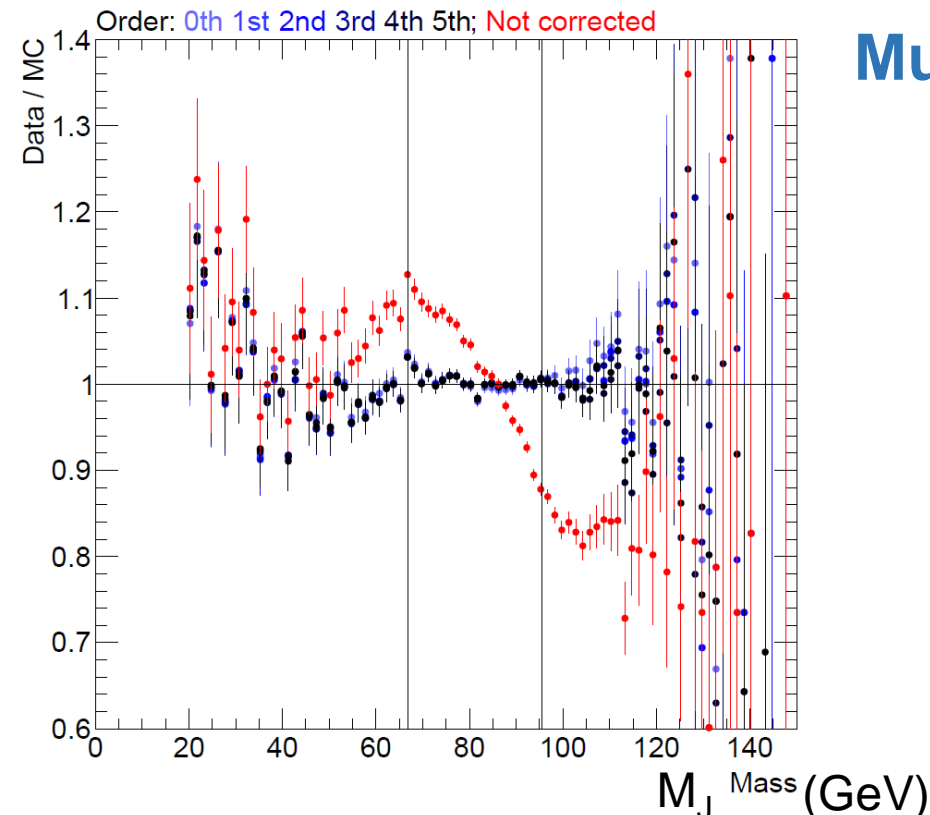
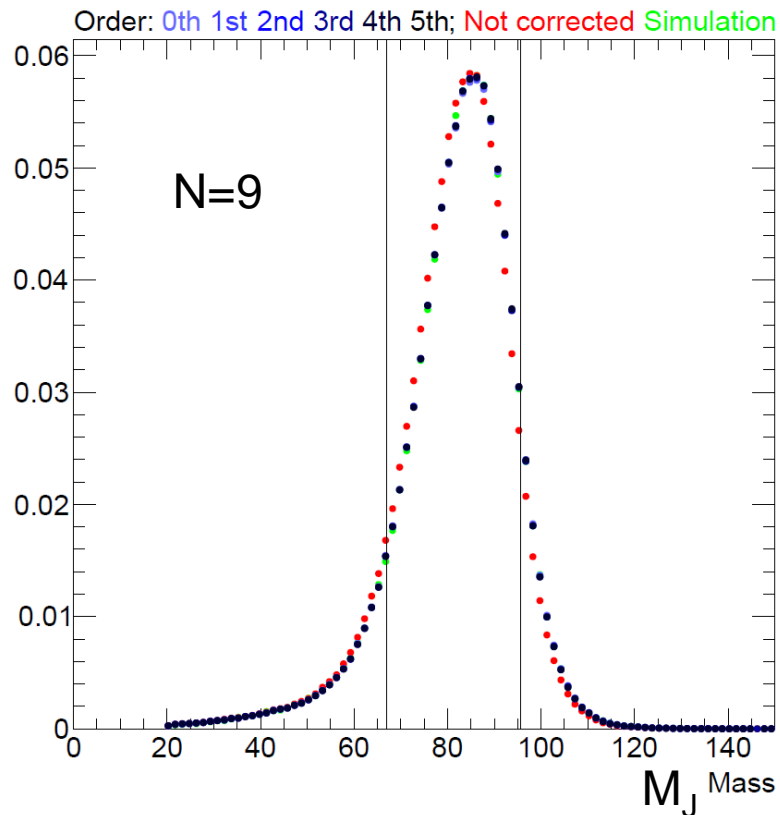
# Data-based Calibration: Relative Plus/Minus Difference



- The second step is to remove the difference in jet energy scale between the **+ side** and **- side**
- Differences in average jet energy in the **+ side**  $\langle E+ \rangle$  and **- side**  $\langle E- \rangle$  is corrected

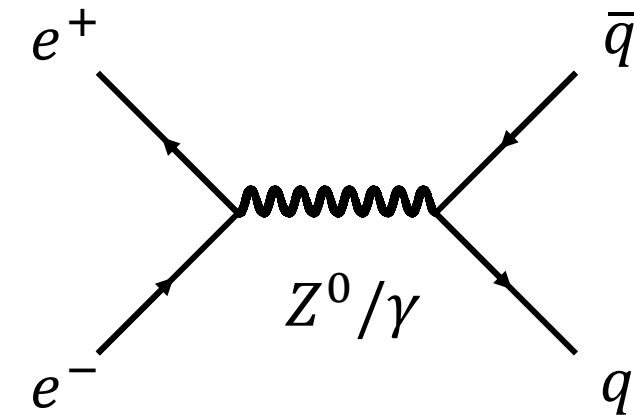


# Data-based Calibration: Absolute Scale



## Multi-jet invariant mass $M_J$ method

Peak at  $M_J = Z^0$  mass

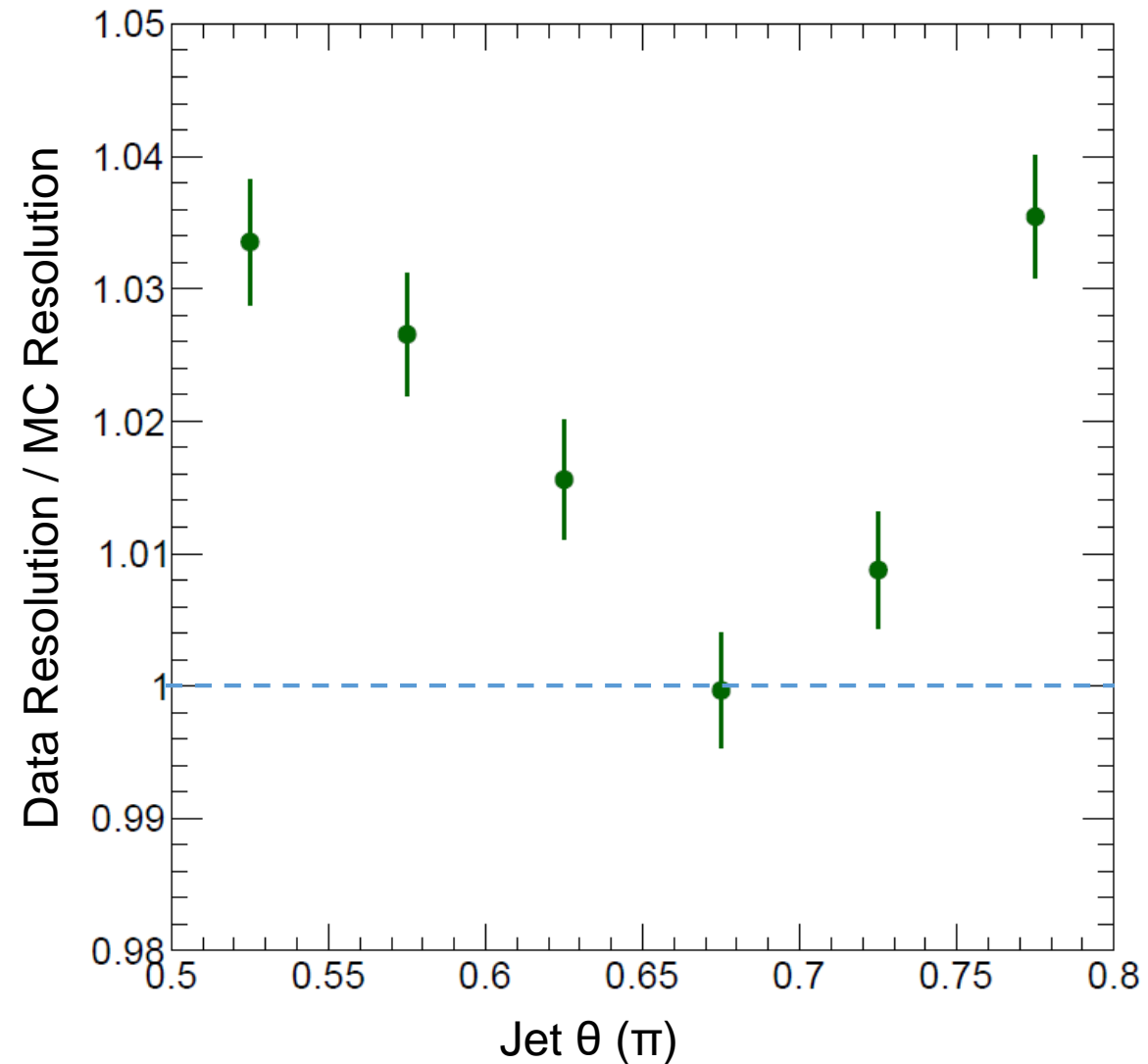
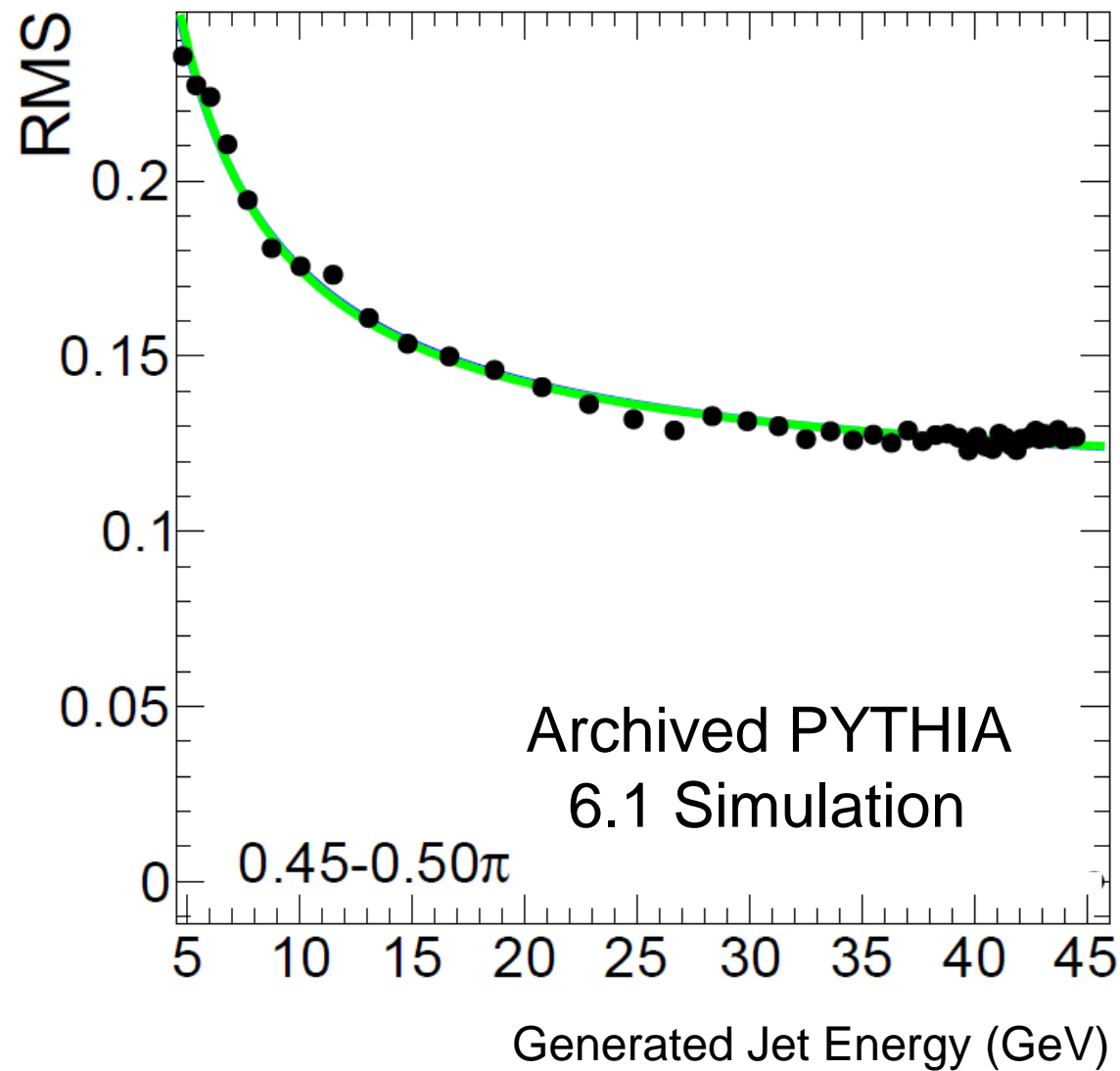


Yi Chen  
(MIT, CMS)

- Performance with up to **N=9** leading jets is presented (ranked by energy)
  - Require  **$(N+1)^{\text{th}}$  jet energy  $< E_{\text{cut}}$**  to reduce the sensitivity to soft jets, where  $E_{\text{cut}}$  is set to 3 GeV
  - N** and  $E_{\text{cut}}$  are varied for systematical uncertainty checks
- Jet energy correction is modeled by  **$n^{\text{th}}$**  order polynomial of the jet energy  **$f(E_{\text{jet}})$**
- Minimize the  $\chi^2$  difference in mean mass between MC and data in 2% quantile ranges (slicing the mass spectrum)
  - 0-10% and 90-100% are removed to minimize impact of outliers
  - n=1 chosen as the nominal correction**

MITHIG-MOD-NOTE-21-001  
[arXiv:2108.04877](https://arxiv.org/abs/2108.04877)

# Jet Energy Resolution



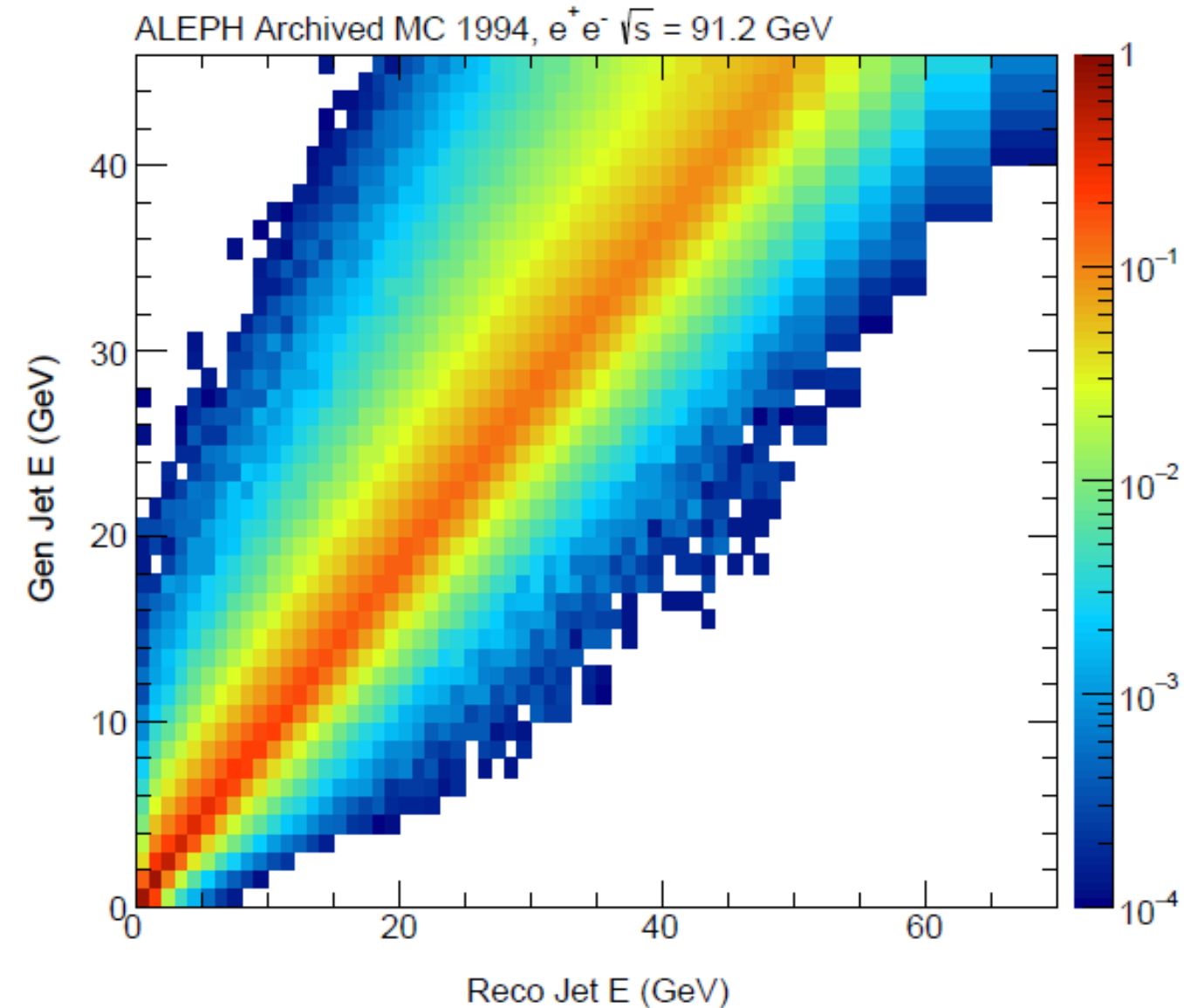
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- Jet energy resolution is around 15-25%
- Difference between data and MC are studied by leading dijet ( 0% ~ 4%)

MITHIG-MOD-NOTE-21-001  
[arXiv:2108.04877](https://arxiv.org/abs/2108.04877)

# Unfolding

- Performed using the ROOUNFOLD package (v2.0.0). **Bayes Unfold method as the nominal result** and SVD as systematics check
- A flat prior is used in Bayes Unfold (PYTHIA 6.1 MC spectra used as prior for systematic check)
- 1D unfolding is performed for jet energy, leading dijet energy spectra.
- For jet mass,  $Z_G$ ,  $R_G$  and groomed mass, 2D unfolding of the observables in bins of jet energy is performed



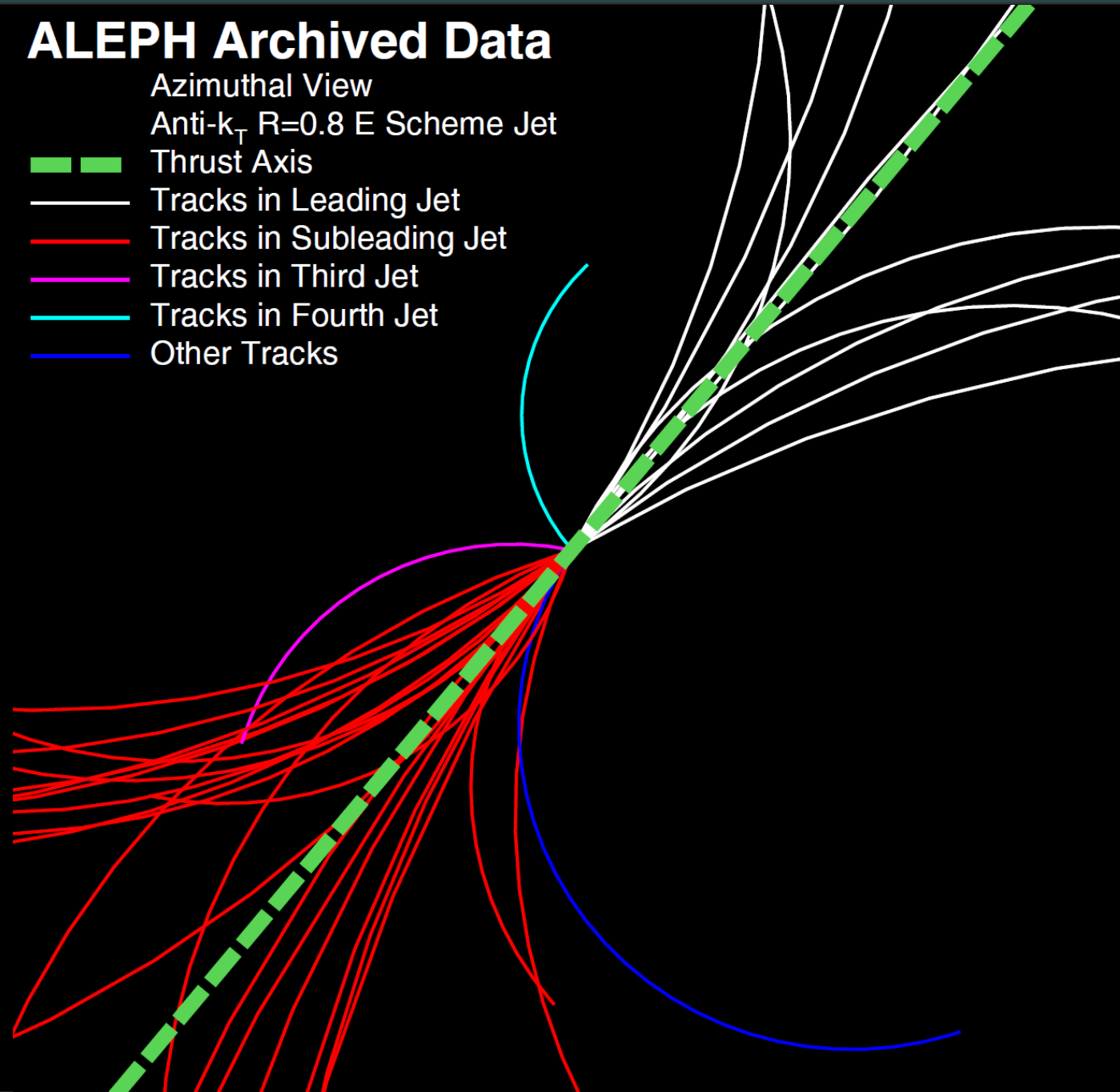
MITHIG-MOD-NOTE-21-001  
[arXiv:2108.04877](https://arxiv.org/abs/2108.04877)



# High Multiplicity Event in $e^+e^-$ Collisions

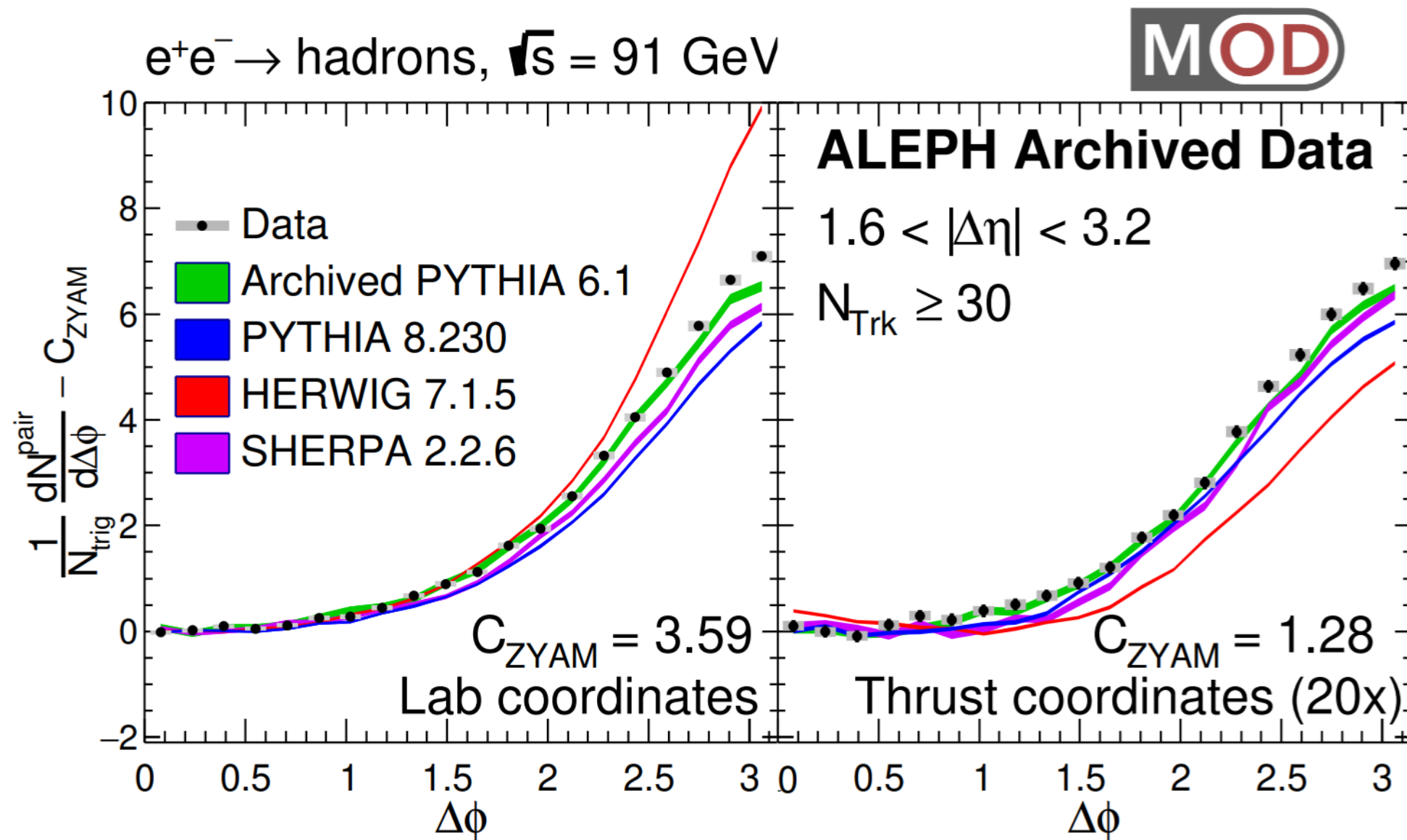
## ALEPH Archived Data

- Azimuthal View
- Anti- $k_T$   $R=0.8$  E Scheme Jet
- Thrust Axis
- Tracks in Leading Jet
- Tracks in Subleading Jet
- Tracks in Third Jet
- Tracks in Fourth Jet
- Other Tracks

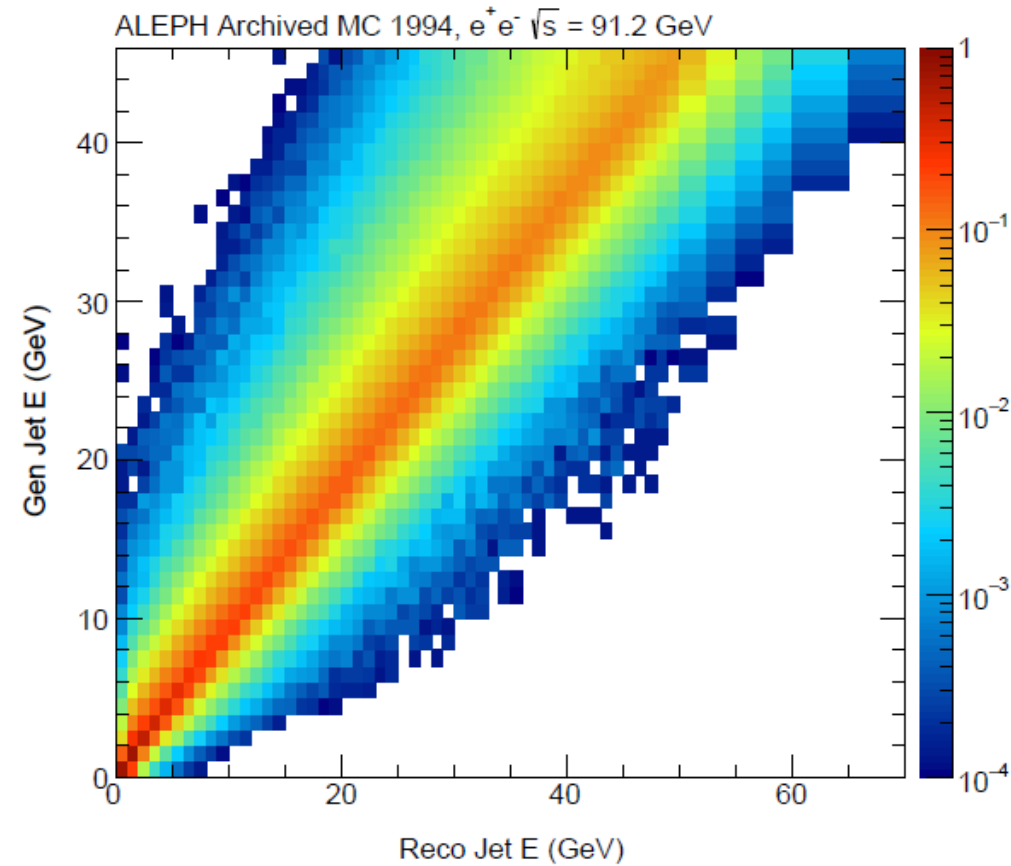
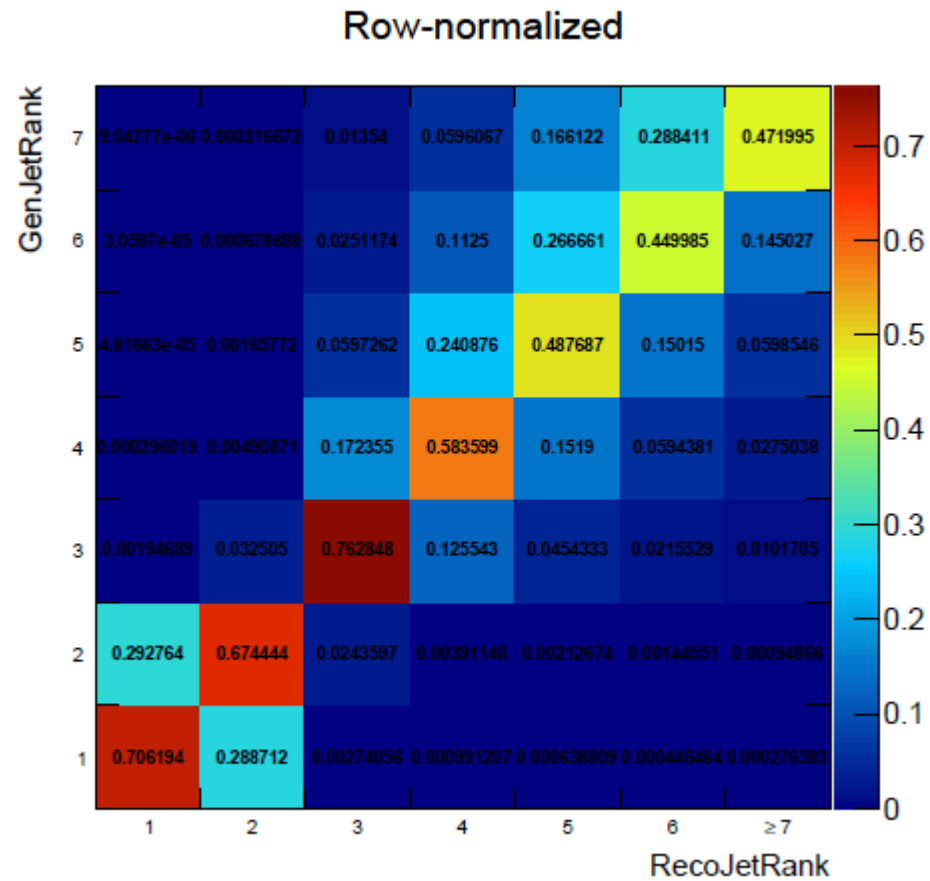


39 Tracks  
 $T=0.98$

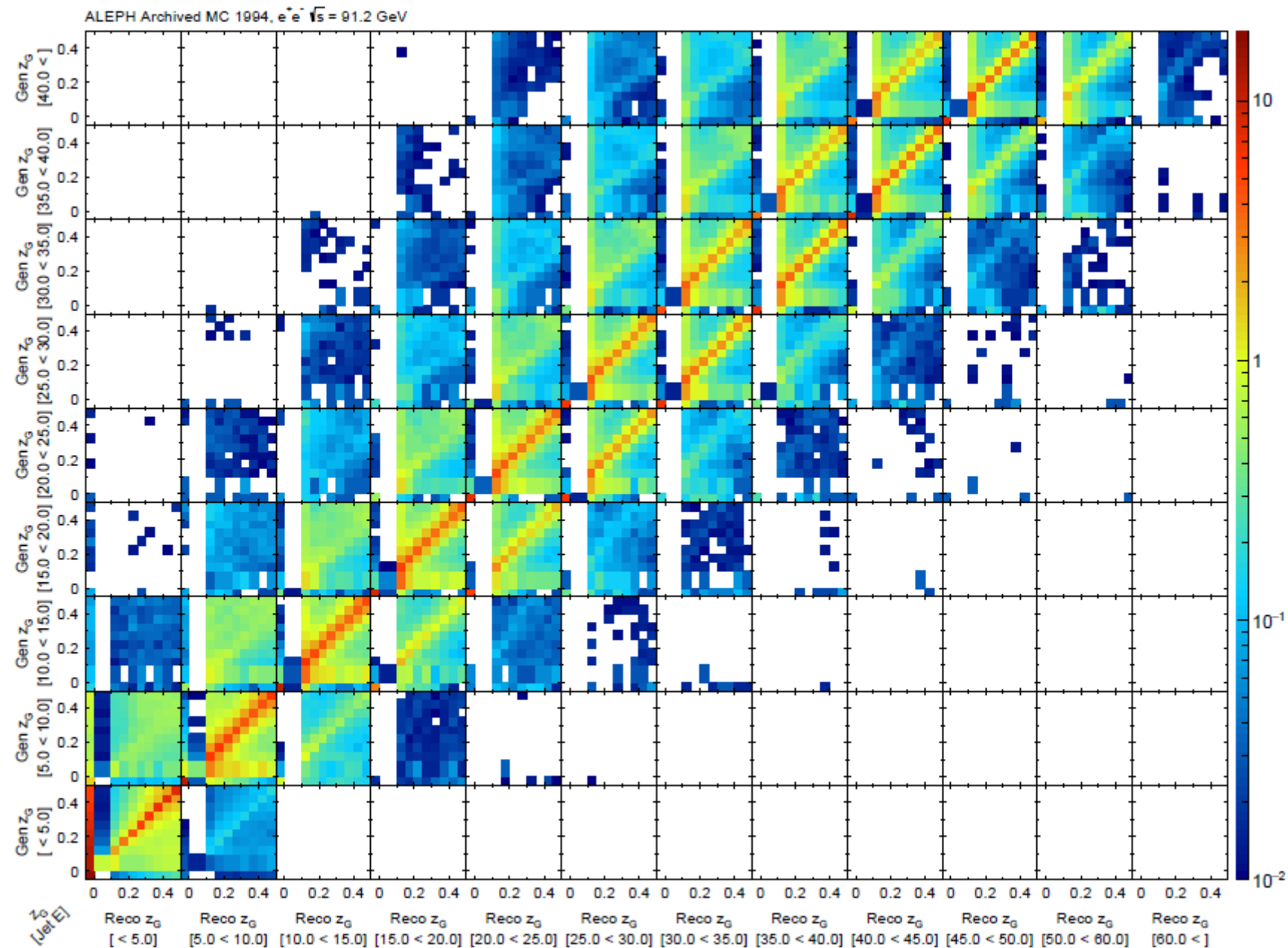
# Correlation Function vs. Generators



# Unfolding

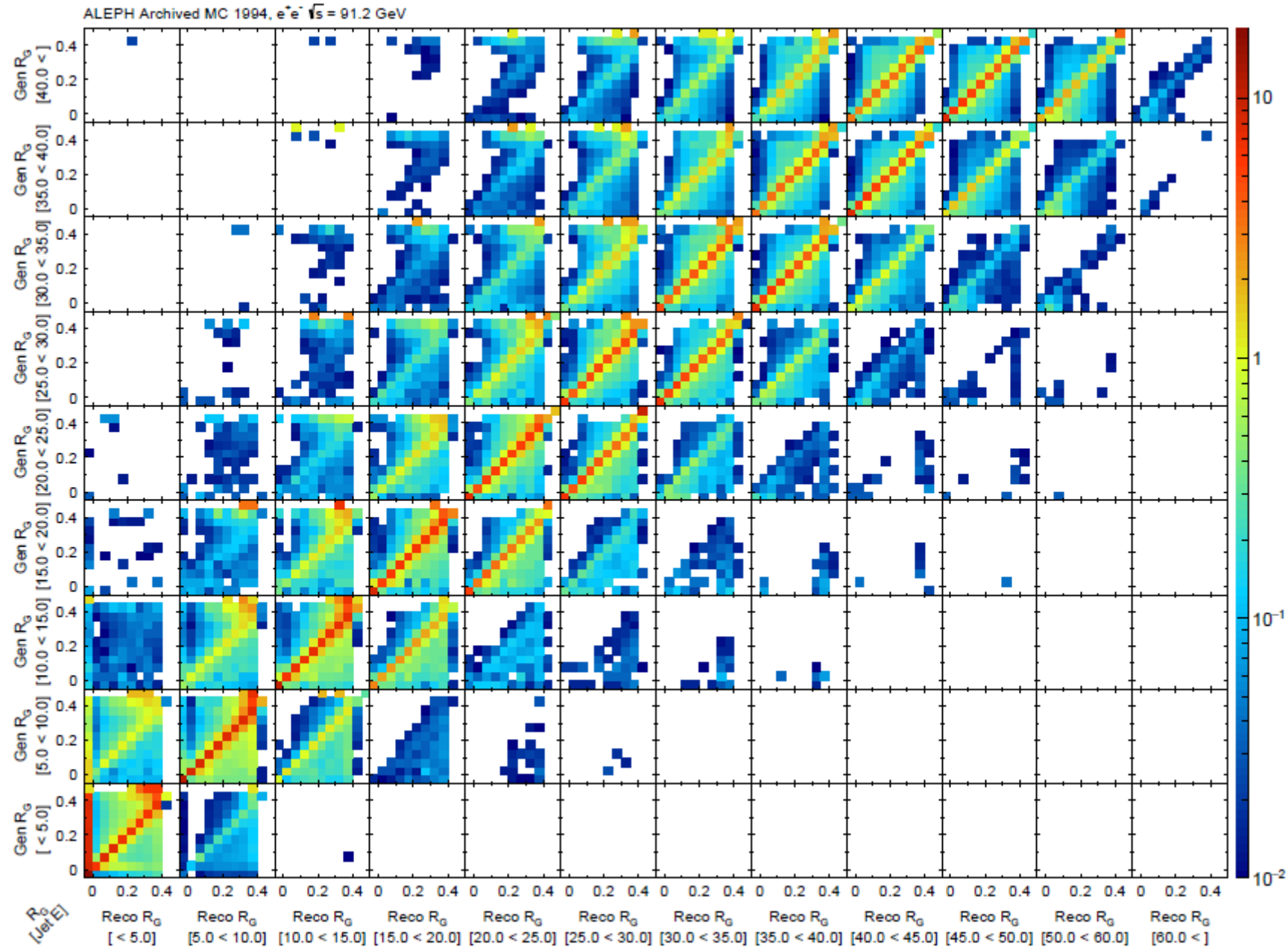


# Response Matrix for $Z_G$

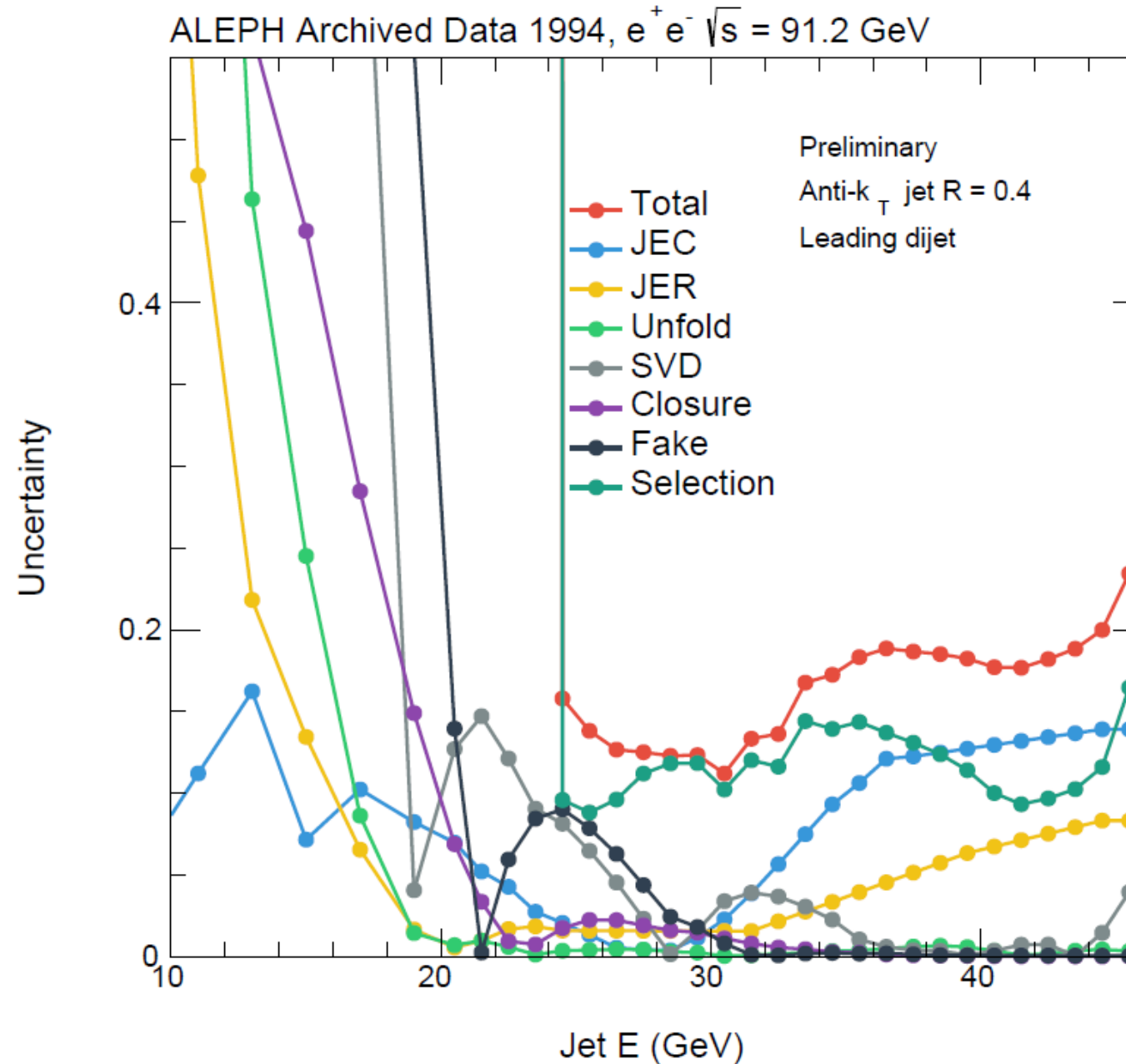




# Response Matrix for $R_G$



# Systematics: Leading Dijet Energy



# Summary of $M_J$ studies

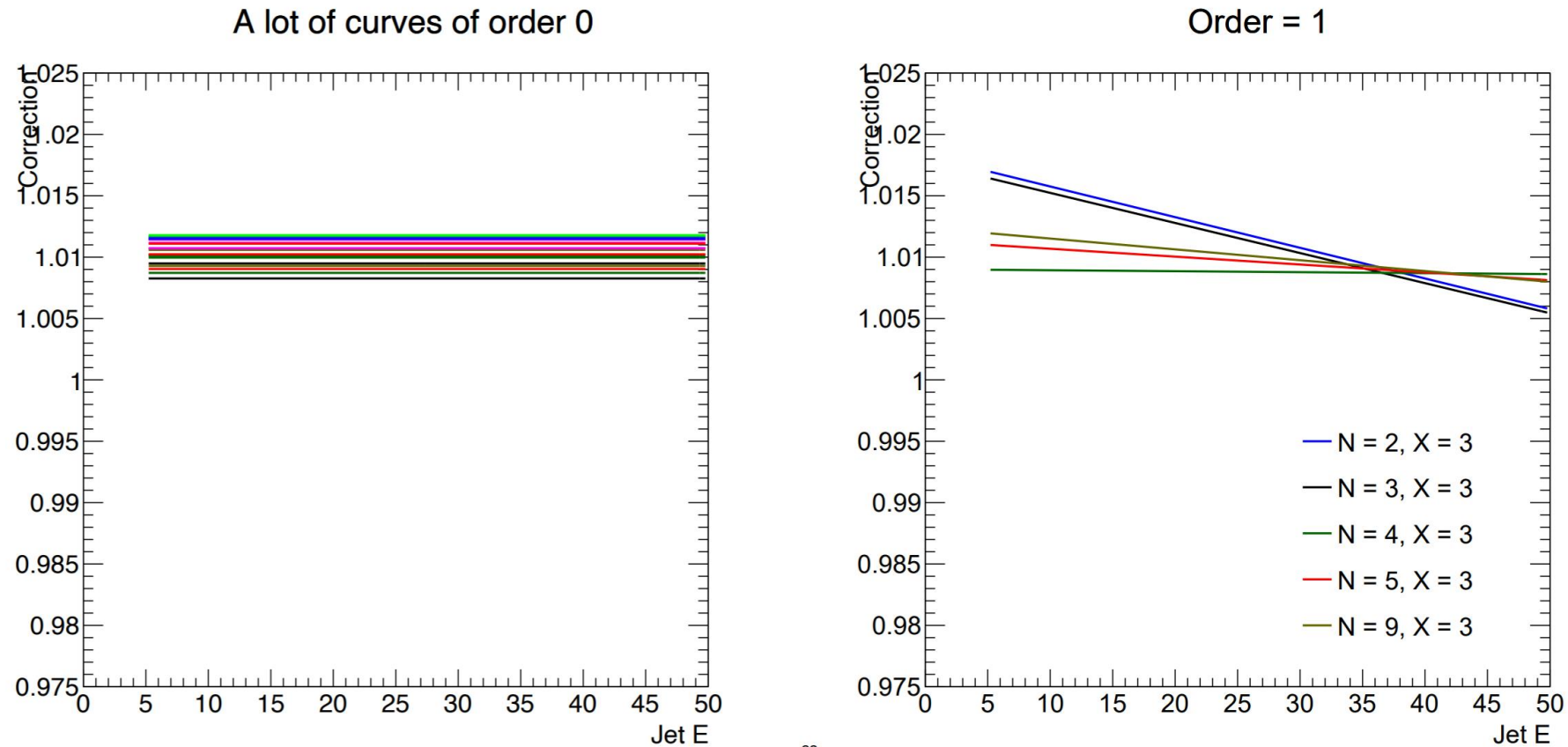


Figure 11: Example of fitted corrections with order 0 (left) and 1 (right). All variations of  $N$  and  $X$  agree for 0-th order fits, and there is a dependence on number of jets  $N$  at low energy.